

Syntax-Directed Translation and Intermediate Code Generation

Chapter 6

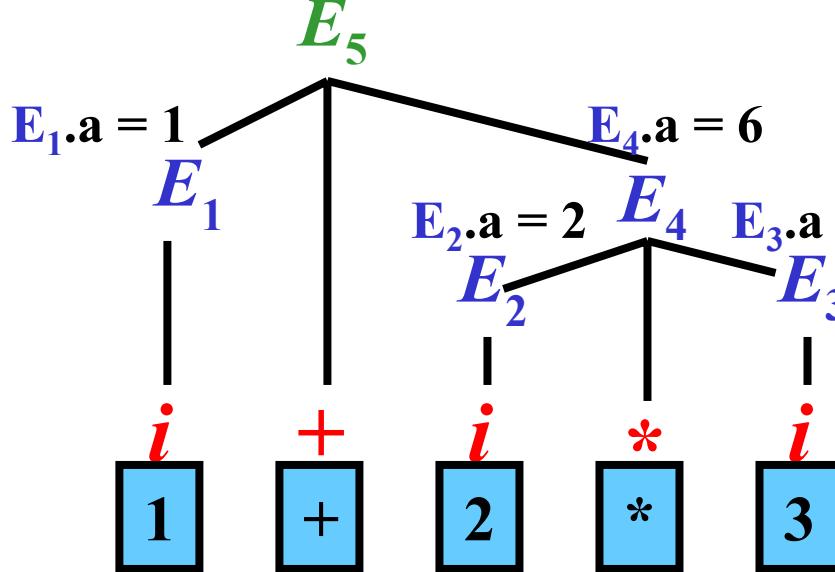
Syntax-Directed Translation

Gist: *Semantic actions* are attached to grammatical rules. Most importantly, these actions make intermediate code generation and type checking.

Example:

$$E_5.a = 7$$

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	$\{ E_i.a := E_j.a + E_k.a \}$
$E_i \rightarrow E_j * E_k$	$\{ E_i.a := E_j.a * E_k.a \}$
$E_i \rightarrow (E_j)$	$\{ E_i.a := E_j.a \}$
$E_i \rightarrow i$	$\{ E_i.a := i.val \}$



Rule:	Action:
$E_1 \rightarrow i$	$E_1.a := i.val$
$E_2 \rightarrow i$	$E_2.a := i.val$
$E_3 \rightarrow i$	$E_3.a := i.val$
$E_4 \rightarrow E_2 * E_3$	$E_4.a := E_2.a * E_3.a$
$E_5 \rightarrow E_1 + E_4$	$E_5.a := E_1.a + E_4.a$

Intermediate Code: Three–Address Code

- Instruction in **three–address code (3AC)** has the form:

(**o**, **→ a**, **→ b**, **→ r**)

- **o** – operator ($+, -, *, \dots$)
- **a** – operand 1 ($\rightarrow a$ = address of **a**)
- **b** – operand 2 ($\rightarrow b$ = address of **b**)
- **r** – result ($\rightarrow r$ = address of **r**)

Examples:

- (**:=** , **a**, , **c**) ... $c := a$
- (**+** , **a**, **b**, **c**) ... $c := a + b$
- (**not** , **a**, , **b**) ... $b := \text{not}(a)$
- (**goto** , , , **L1**) ... *goto L1*
- (**goto** , **a**, , **L1**) ... *if a = true then goto L1*
- (**lab** , **L1**, ,) ... *label L1:*

Syntax-Directed Generation of 3AC

Basic approaches:

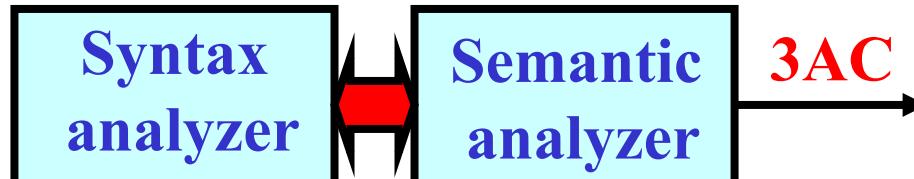
- 1) Parser directs the creation of an *abstract-syntax tree (AST)*, which is then converted to **3AC**.



- 2) Parser directs the creation of a *postfix notation (PN)*, which is then converted to **3AC**.



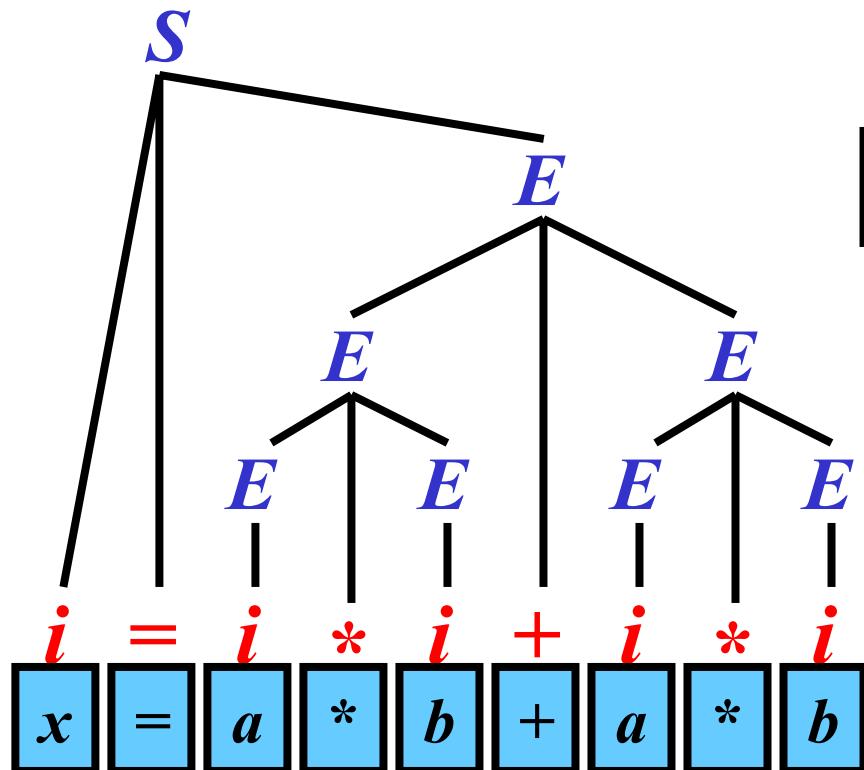
- 3) A parser directs the creation of **3AC**.



From a Parse Tree (PT) to an AST: Example

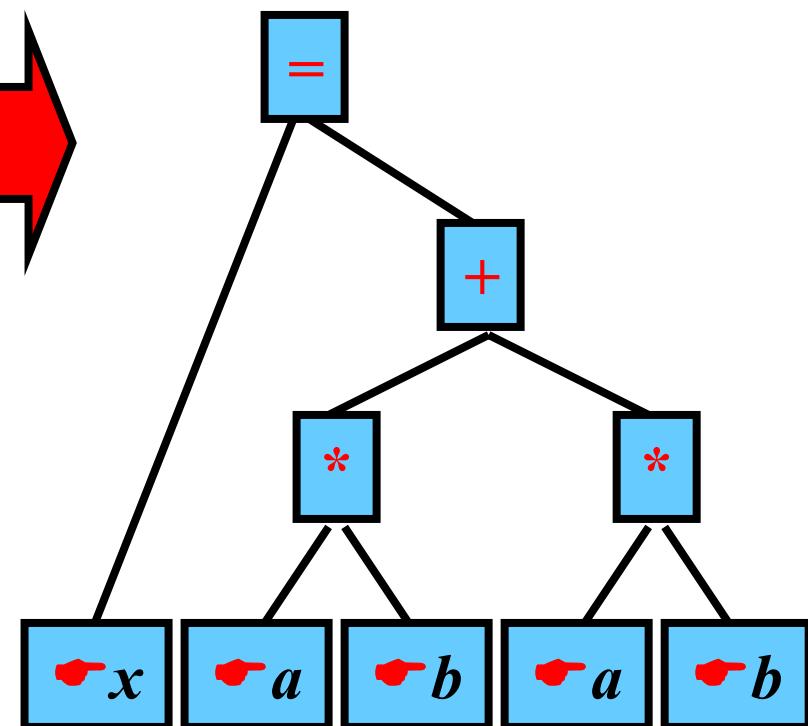
- PT for

$x = a^*b + a^*b:$



- AST for

$x = a^*b + a^*b:$



Generation of AST

Gist: A parser simulates the construction of PT and, simultaneously, calls some semantic actions to create AST.

Example:

Rule:	Semantic Action:
$S \rightarrow i := E_k$	$\{ S.a := \text{MakeTree}('=', i.a, E_k.a) \}$
$E_i \rightarrow E_j + E_k$	$\{ E_i.a := \text{MakeTree}('+', E_j.a, E_k.a) \}$
$E_i \rightarrow E_j * E_k$	$\{ E_i.a := \text{MakeTree}('*', E_j.a, E_k.a) \}$
$E_i \rightarrow (E_j)$	$\{ E_i.a := E_j.a \}$
$E_i \rightarrow i$	$\{ E_i.a := \text{MakeLeaf}(i.a) \}$

Notes:

- $\text{MakeTree}(o, a, b)$ creates a new node o , attaches sons a (left) and b , and returns a pointer to node o
- $\text{MakeLeaf}(i.a)$ creates a new node $i.a$ ($i.a$ is a symbol-table address) and returns a pointer to this new node

AST Generation: Example 1/2

Pushdown	Input	Rule	Semantic action
\$	$i = (i + i) * i \$$		
\$i	$= (i + i) * i \$$		
\$i =	$(i + i) * i \$$		
\$i = ($i + i) * i \$$		
\$i = (i	$+ i) * i \$$	$E_1 \rightarrow i$	$E_1.a := \text{MakeLeaf}(i.a)$
\$i = (E_1	$+ i) * i \$$		
\$i = (E_1 +	$i) * i \$$		
\$i = (E_1 + i	$) * i \$$	$E_2 \rightarrow i$	$E_2.a := \text{MakeLeaf}(i.a)$
\$i = (E_1 + E_2	$) * i \$$	$E_3 \rightarrow E_1 + E_2$	$E_3.a := \text{MakeTree}('+', E_1.a, E_2.a)$
\$i = (E_3	$) * i \$$		
\$i = (E_3)	$* i \$$	$E_4 \rightarrow (E_3)$	$E_4.a := E_3.a$
\$i = E_4	$* i \$$		
\$i = E_4 *	$i \$$		
\$i = E_4 * i	$\$$	$E_5 \rightarrow i$	$E_5.a := \text{MakeLeaf}(i.a)$
\$i = E_4 * E_5	$\$$	$E_6 \rightarrow E_4 * E_5$	$E_6.a := \text{MakeTree}('*', E_4.a, E_5.a)$
\$i = E_6	$\$$	$S \rightarrow i = E_6$	$S.a := \text{MakeTree}('=', i.a, E_6.a)$
\$\$S	$\$$		

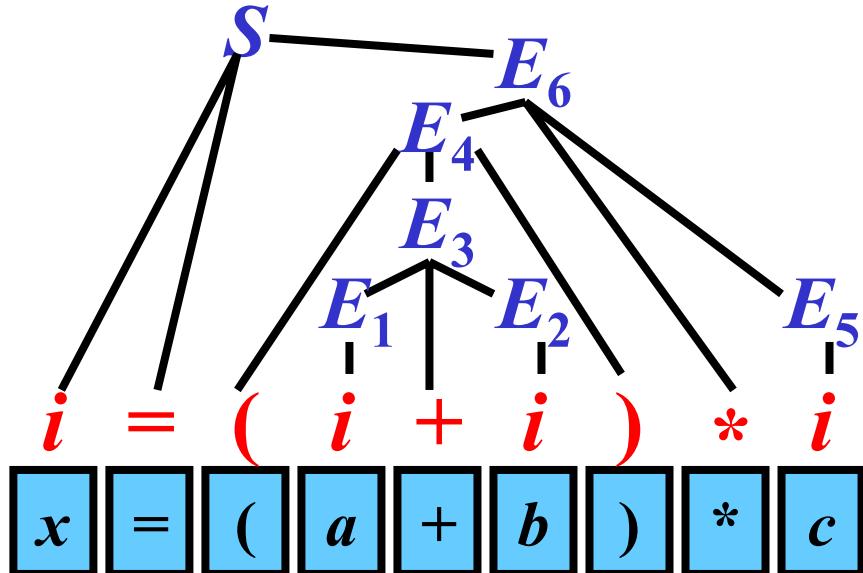
Bottom-Up parsing

Semantic actions

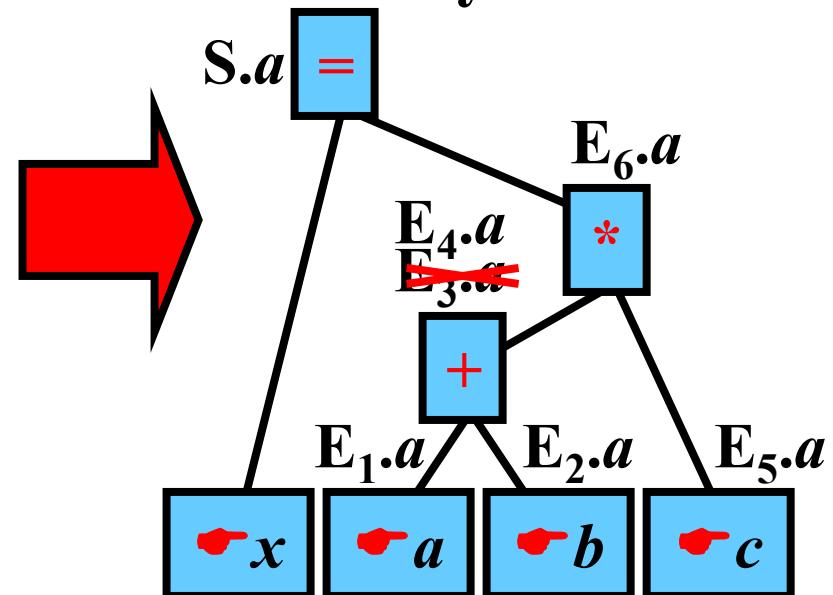
AST Generation: Example 2/2

Rule:	Semantic Action:
$E_1 \rightarrow i$ $E_2 \rightarrow i$ $E_3 \rightarrow E_1 + E_2$ $E_4 \rightarrow (E_3)$ $E_5 \rightarrow i$ $E_6 \rightarrow E_4 * E_5$ $S \rightarrow i = E_6$	$E_1.a := \text{MakeLeaf}(i.a)$ $E_2.a := \text{MakeLeaf}(i.a)$ $E_3.a := \text{MakeTree}('+' , E_1.a, E_2.a)$ $E_4.a := E_3.a$ $E_5.a := \text{MakeLeaf}(i.a)$ $E_6.a := \text{MakeTree}('*' , E_4.a, E_5.a)$ $S.a := \text{MakeTree}('=' , i.a, E_6.a)$

Simulated Parse tree:



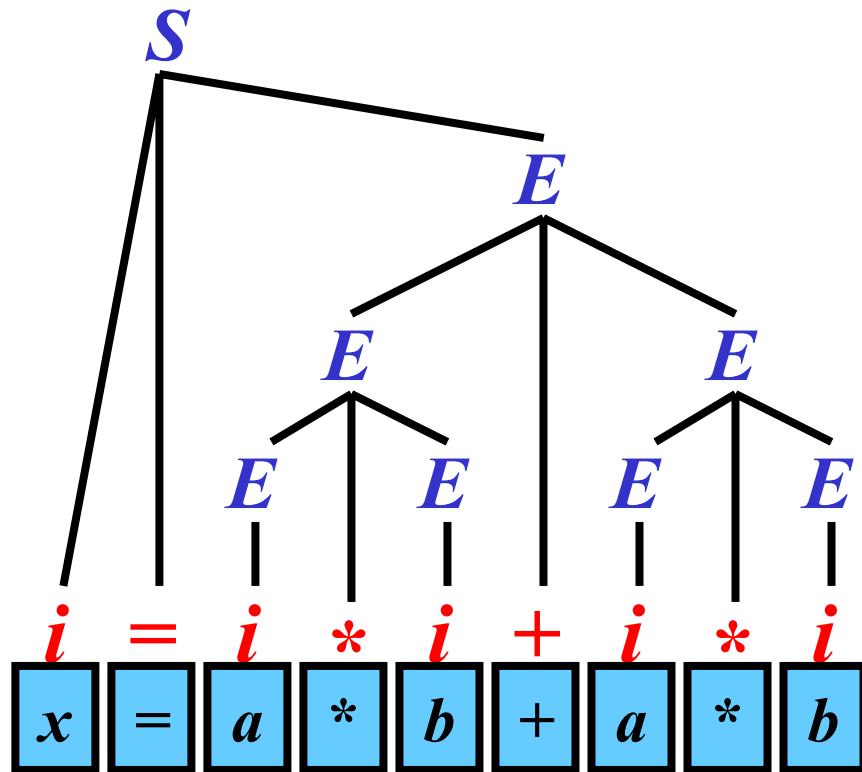
Abstract syntax tree:



Direct Acyclic Graph(DAG): Example

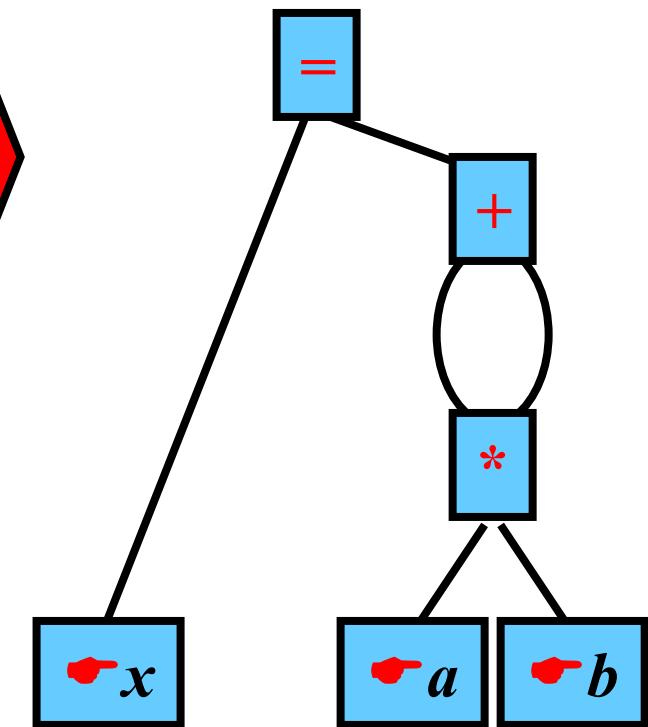
- Parse tree for

$$x = a^*b + a^*b:$$



- DAG for

$$x = a^*b + a^*b:$$



Note: DAG has no redundant nodes.

Postfix Notation

Gist: Every operator occurs behind its operands.

Example:

Infix notation	Postfix notation
$a + b$	$a\ b\ +$
$a = b$	$a\ b\ =$
if C then S_1 else S_2	$C\ S_1\ S_2\ \text{if-then-else}$

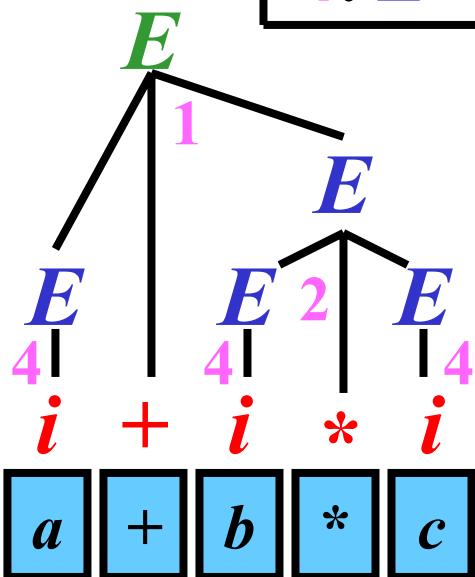
Note: Postfix notation is achievable by the postorder traversal of AST.

Infix to Postfix Directed by a BU Parser

Gist: Semantic actions produce the postfix version of the tokenized source program.

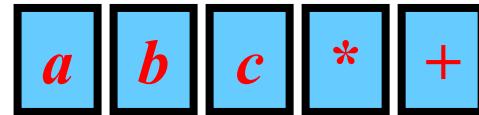
Example:

Rule:	Semantic Action:
1: $E \rightarrow E+E$	{generate('+')}
2: $E \rightarrow E * E$	{generate('*')}
3: $E \rightarrow (E)$	{ - }
4: $E \rightarrow i$	{generate(i.a)}



Input:

Output:



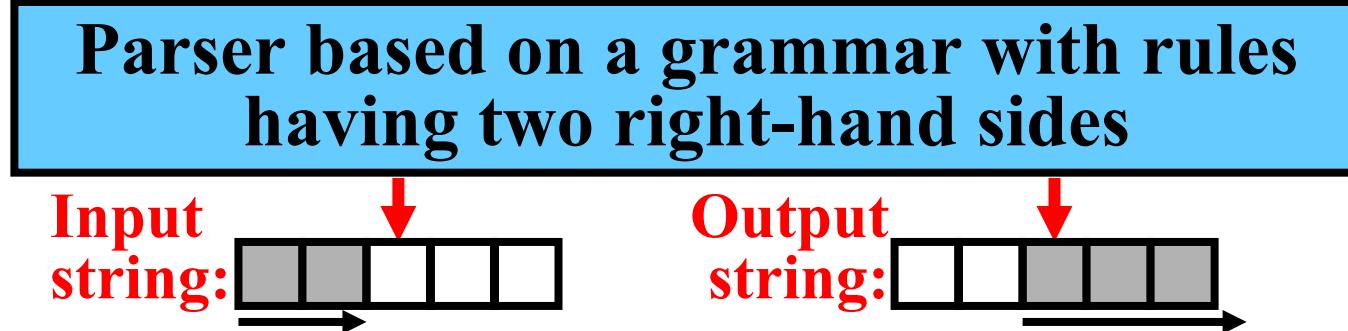
Translation Grammars

Gist: Translation grammars translate input strings to output strings

1) Translation by two grammars:



2) Translation by a single grammar

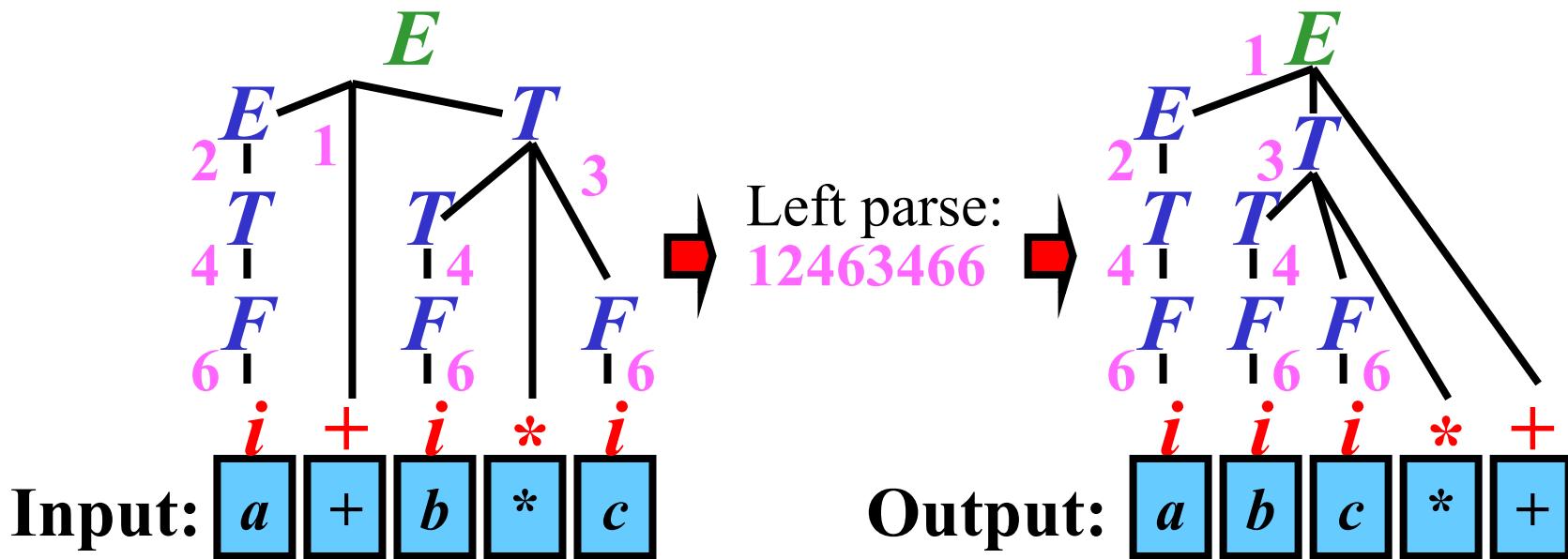


Note: During the parse of an input string, a simultaneous generation of an output string occurs

Two-Grammar Translation

Infix to postfix
translation:

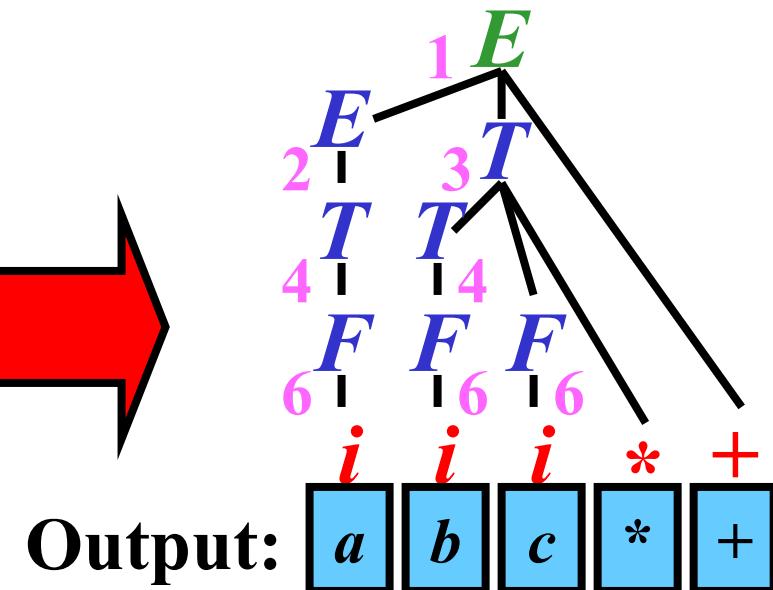
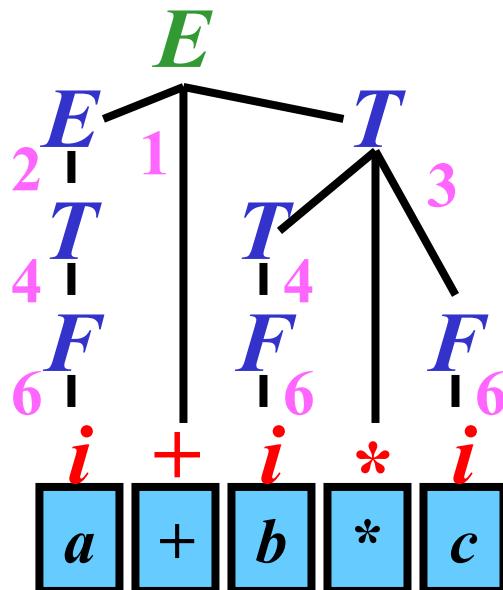
Rules of G ₁	Rules of G ₂
1: $E \rightarrow E + T$	1: $E \rightarrow ET^+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T^* F$	3: $T \rightarrow TF^*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



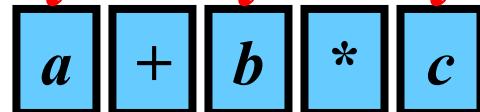
One-Grammar Translation

Infix to postfix
translation:

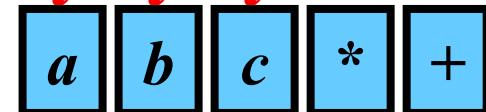
Rule	Tran. Element
1: $E \rightarrow E + T$	$ET+$
2: $E \rightarrow T$	T
3: $T \rightarrow T^* F$	TF^*
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i



Input:



Output:

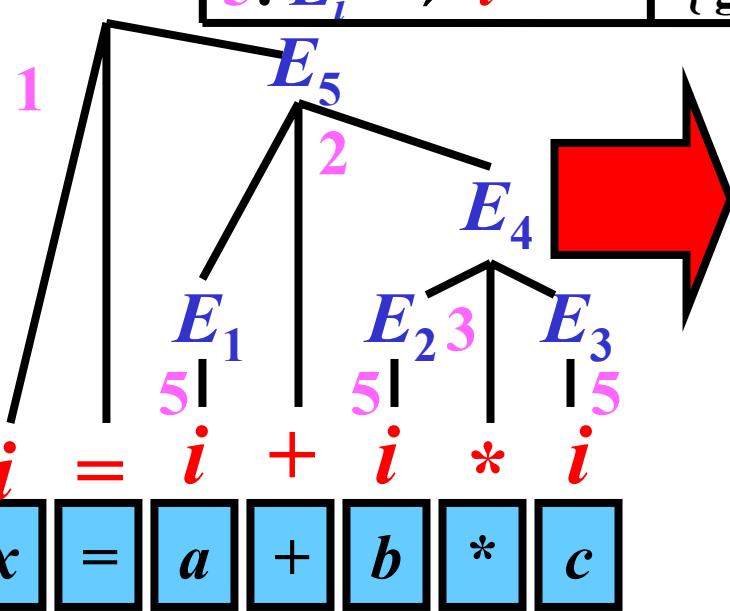


Direct Generation of 3AC

Gist: BU parser directs the generation of 3AC directly.

Example:

Rule:	Semantic Action:
1: $S \rightarrow i = E_k$	{ generate('=', $E_k.loc$, , $i.loc$) }
2: $E_i \rightarrow E_j + E_k$	{ generate('+', $E_j.loc$, $E_k.loc$, $E_i.loc$) }
3: $E_i \rightarrow E_j * E_k$	{ generate('*', $E_j.loc$, $E_k.loc$, $E_i.loc$) }
4: $E_i \rightarrow (E_j)$	{ generate('=', $E_j.loc$, , $E_i.loc$) }
5: $E_i \rightarrow i$	{ generate('=', $i.loc$, , $E_i.loc$) }



Input: x $=$ a $+$ b $*$ c

Output:

- (‘=’, \cancel{a} , , $E_1.loc$)
- (‘=’, \cancel{b} , , $E_2.loc$)
- (‘=’, \cancel{c} , , $E_3.loc$)
- (‘*’, $E_2.loc$, $E_3.loc$, $E_4.loc$)
- (‘+’, $E_1.loc$, $E_4.loc$, $E_5.loc$)
- (‘=’, $E_5.loc$, , \cancel{x})

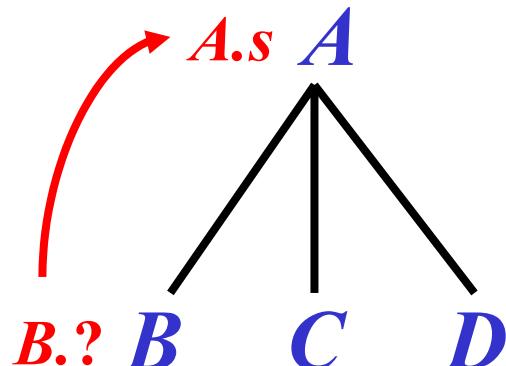
Top-Down Translation: Introduction

- LL-grammar with attributes
- Two pushdown:
 - parser pushdown \times semantic pushdown

- Two type of attributes:

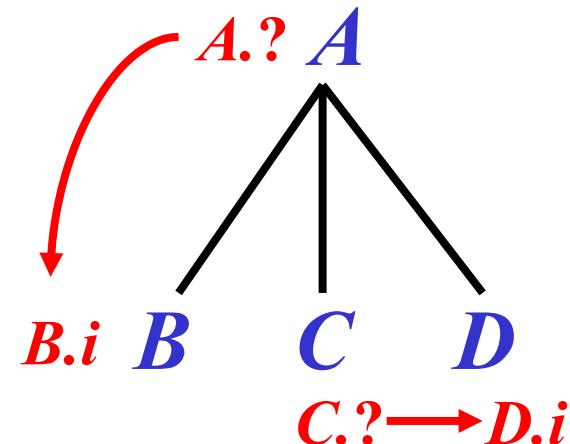
- synthesized:

(from children to parent)



- inherited:

(from parent to children or between siblings)



Top-Down Translation: Expressions

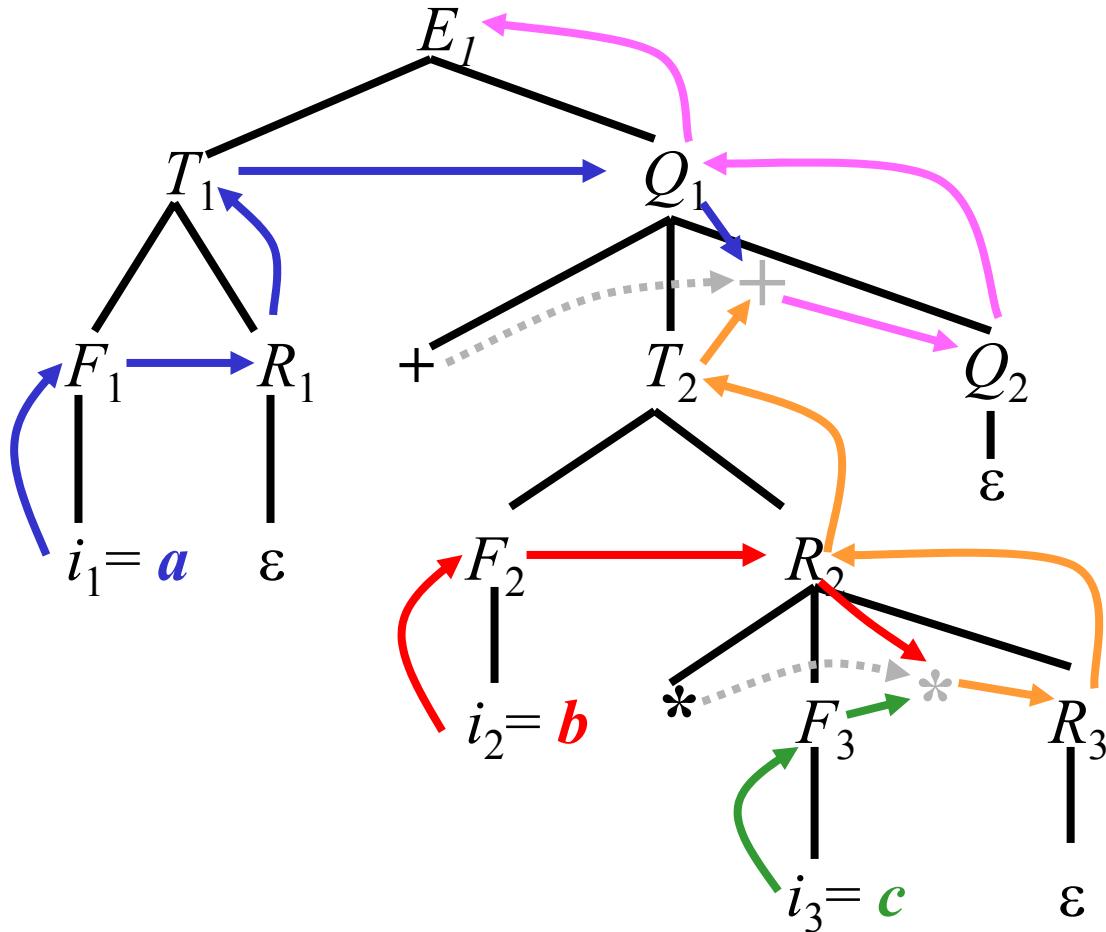
Grammar:

```

 $E \rightarrow TQ$ 
 $Q \rightarrow +TQ$ 
 $Q \rightarrow \varepsilon$ 
 $T \rightarrow FR$ 
 $R \rightarrow *FR$ 
 $R \rightarrow \varepsilon$ 
 $F \rightarrow (E)$ 
 $F \rightarrow i$ 

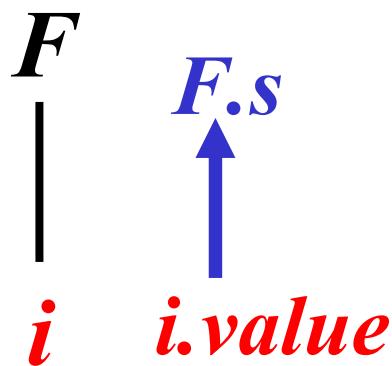
```

Parse tree for $a + b * c$:

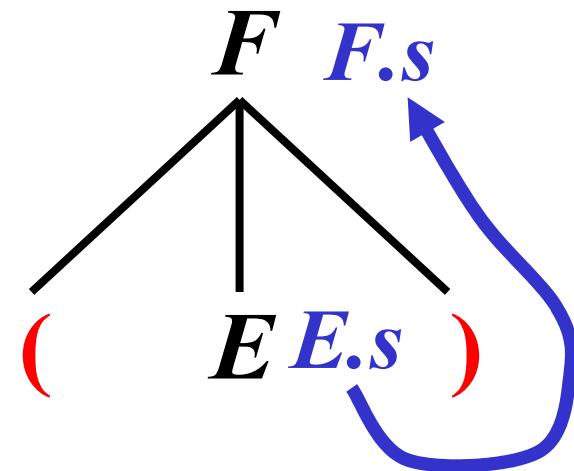


Expressions: Variable & Parentheses

Variable:



Parentheses:

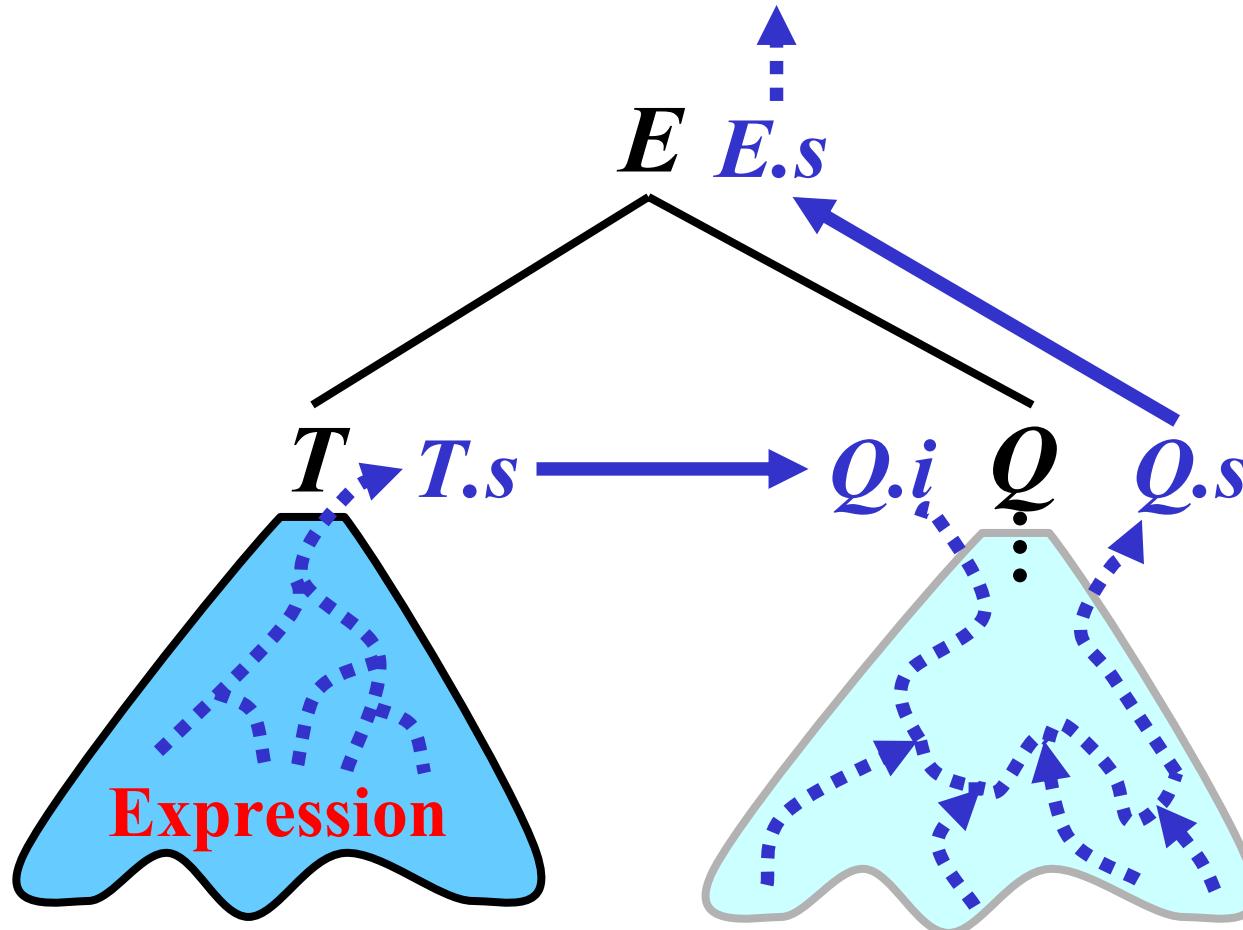


$$F \rightarrow i \{F.s := i.value\}$$

$$E \rightarrow (F \{F.s := E.s\})$$

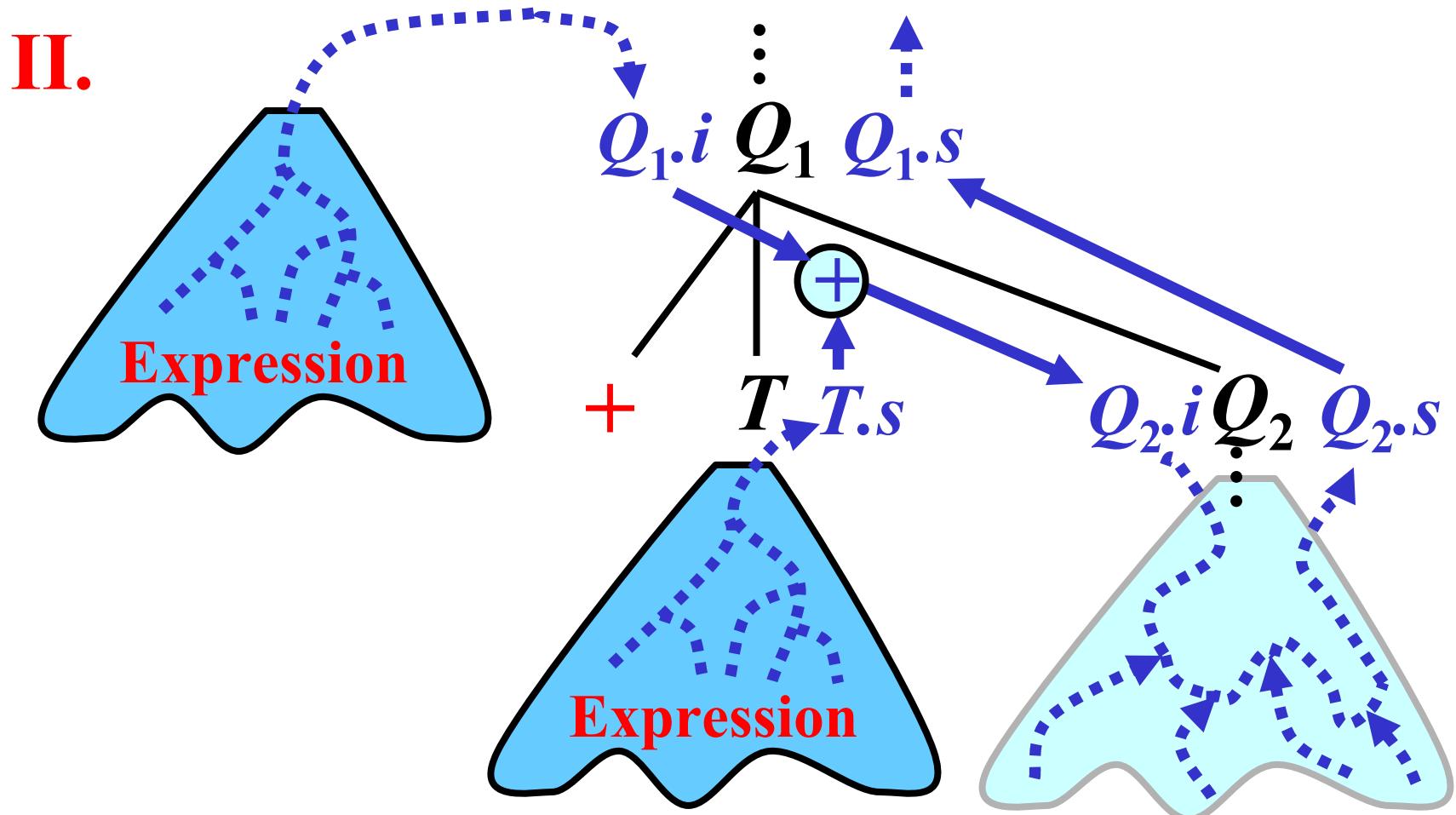
Expressions: Addition 1/4

I.



$$E \rightarrow T \{ Q.i := T.s \} \quad Q \{ E.s := Q.s \}$$

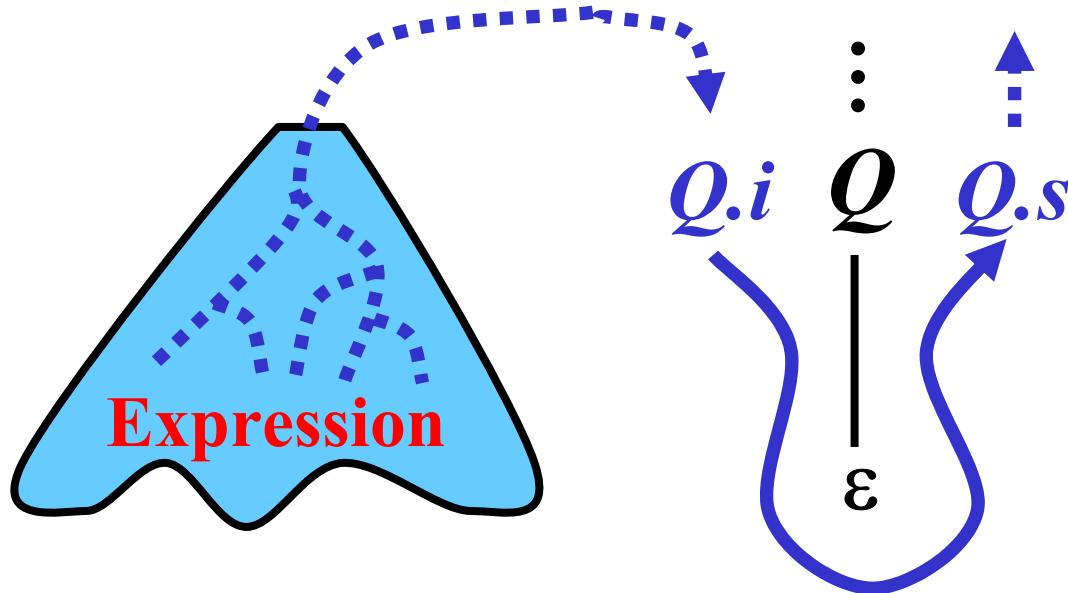
Expressions: Addition 2/4



$$Q_1 \rightarrow +T \{ Q_2.i := Q_1.i + T.s \} Q_2 \{ Q_1.s := Q_2.s \}$$

Expressions: Addition 3/4

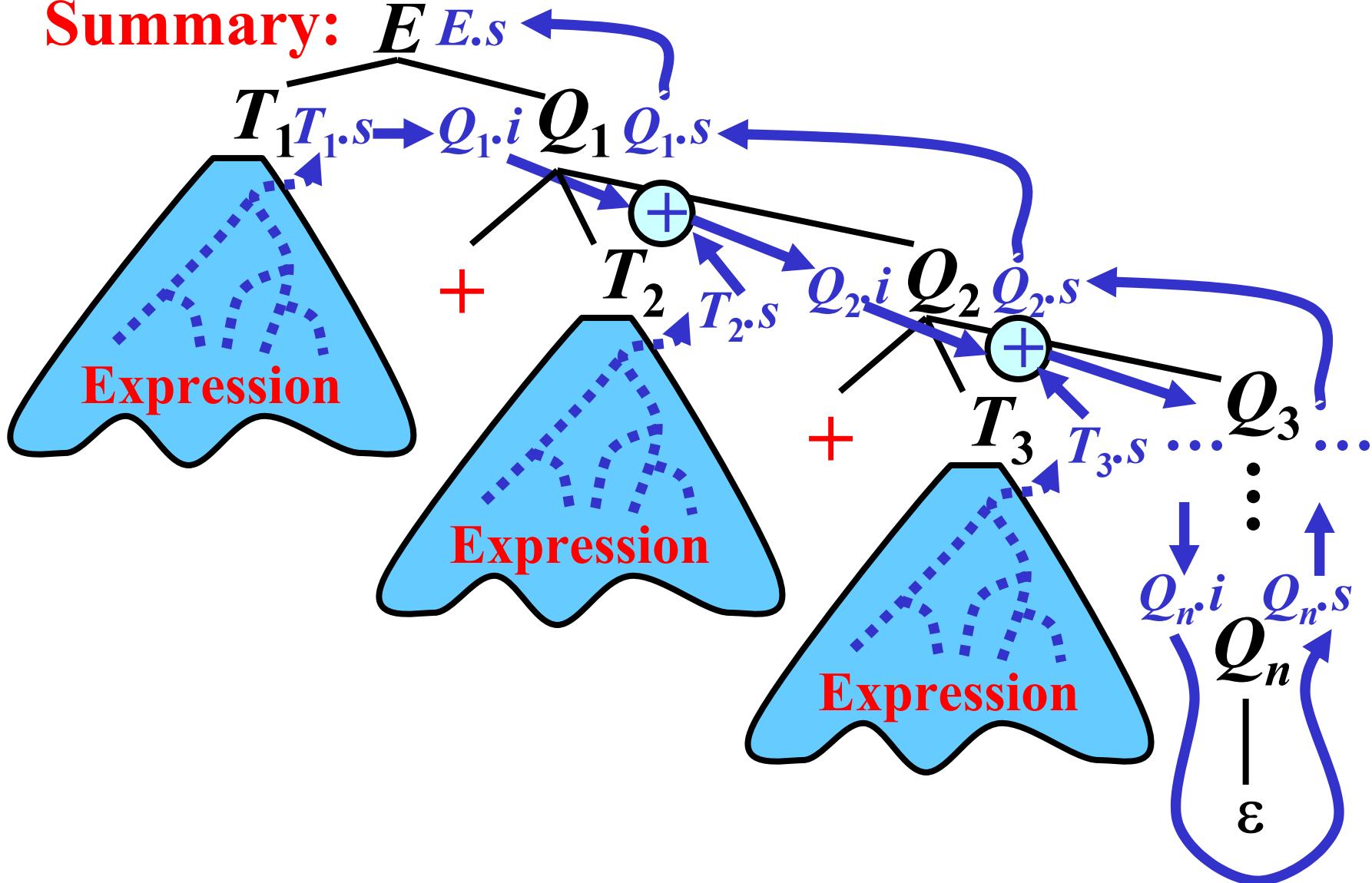
III.



$$Q \rightarrow \varepsilon \quad \{Q.s := Q.i\}$$

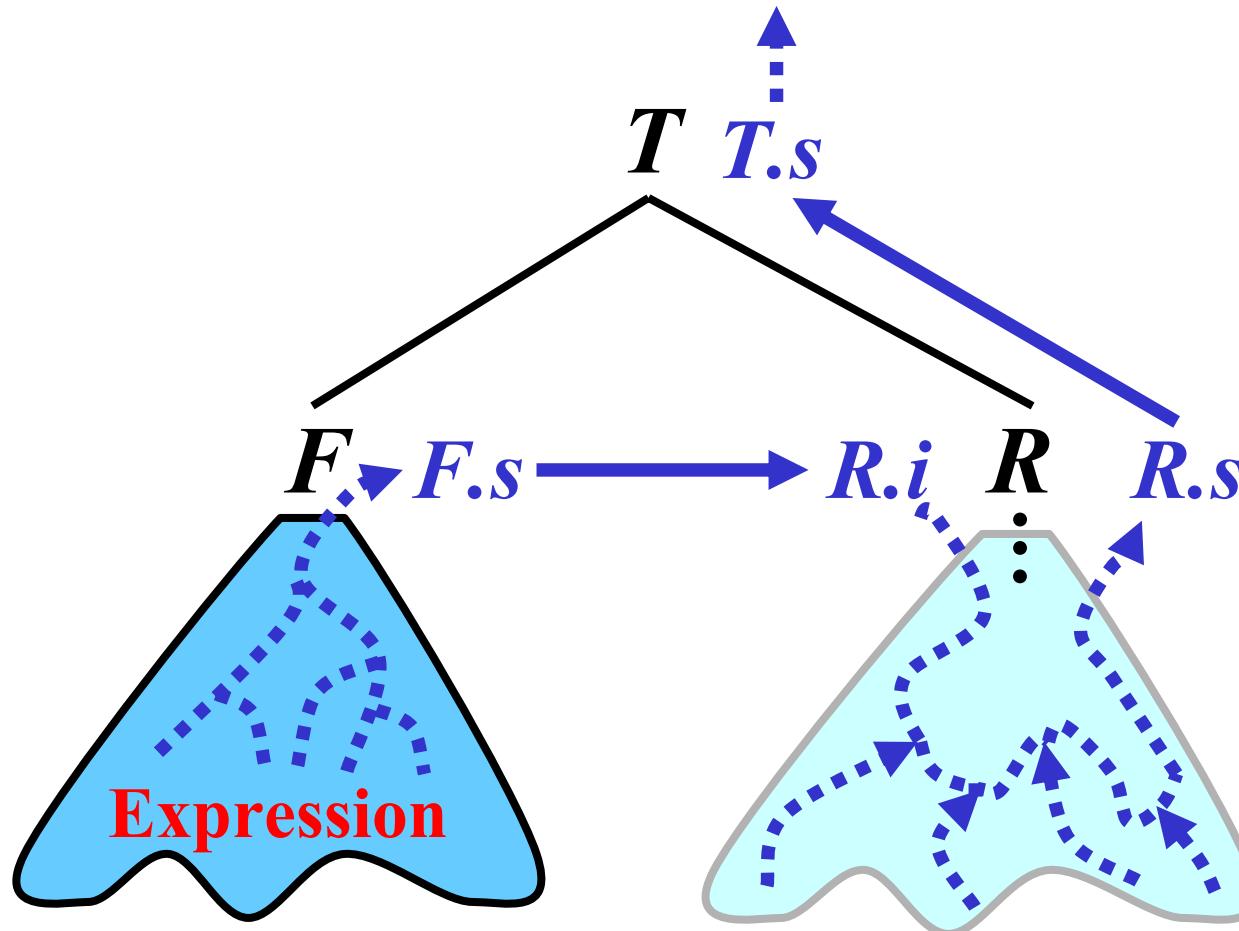
Expressions: Addition 4/4

Summary: $E \xrightarrow{E.s} E$



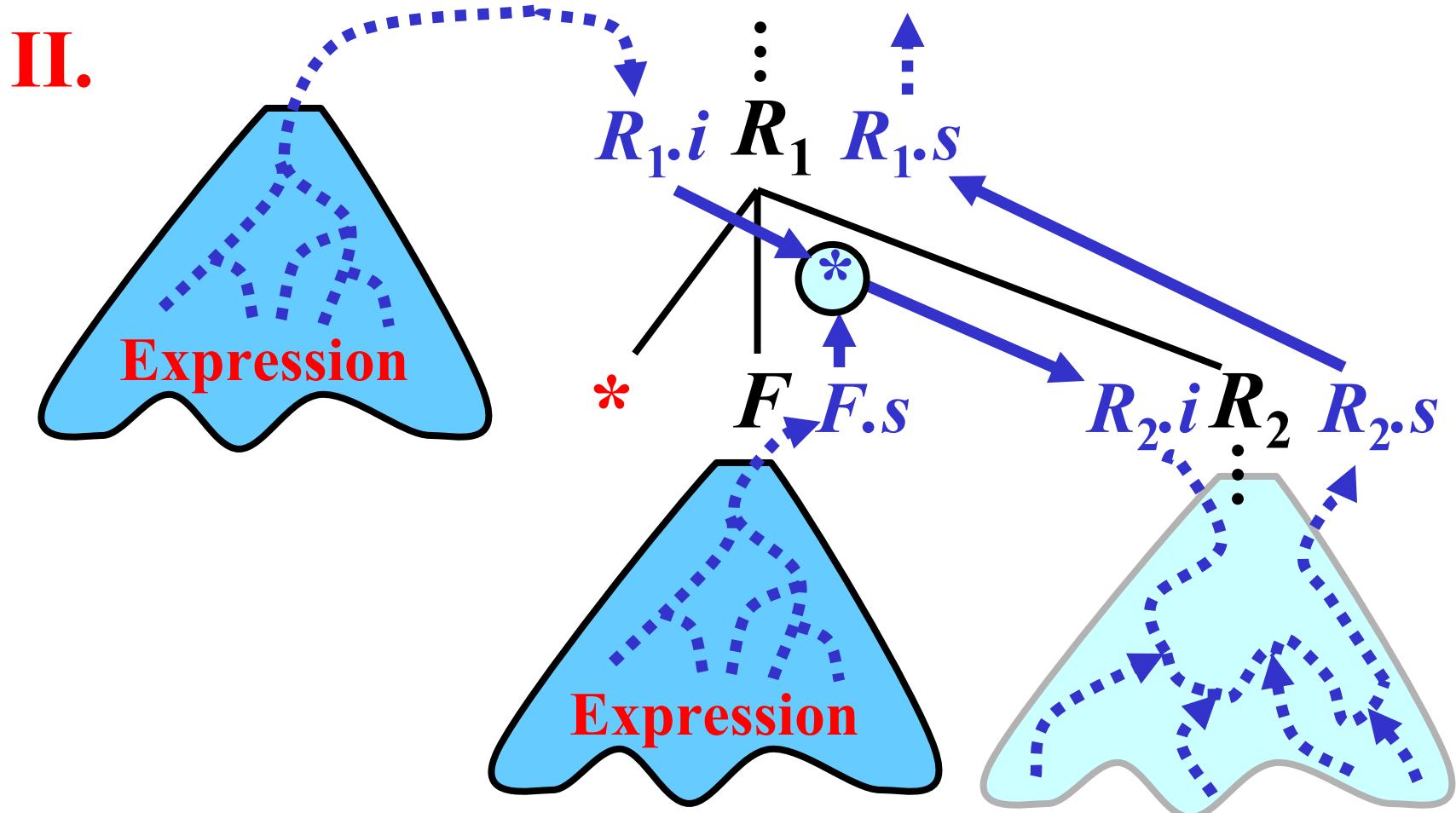
Expressions: Multiplication 1/4

I.



$$T \rightarrow F \{ R.i := F.s \} R \{ T.s := R.s \}$$

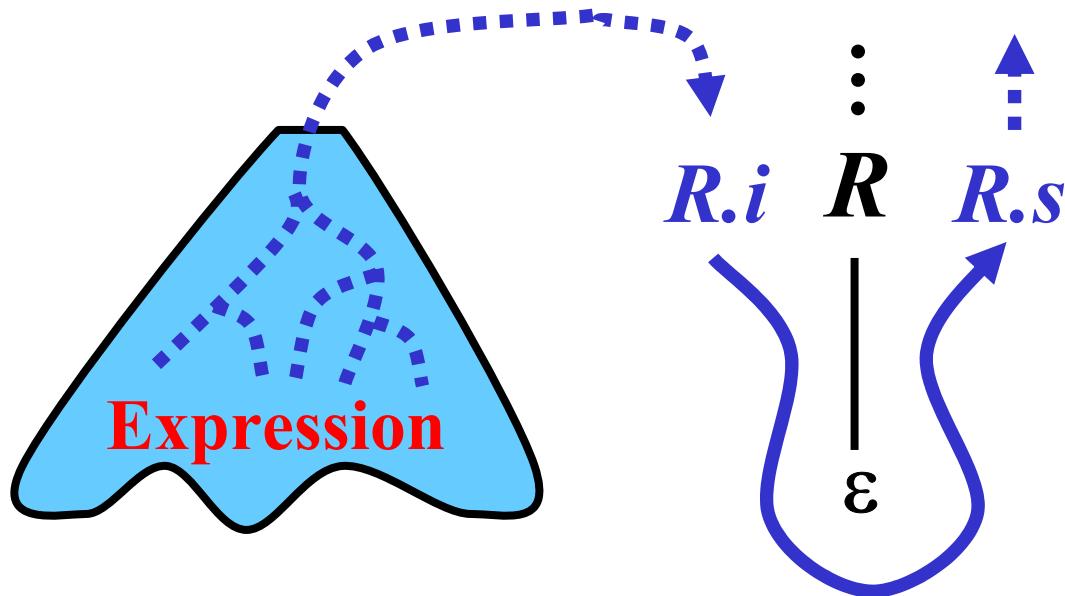
Expressions: Multiplication 2/4



$$R_1 \rightarrow *F \{ R_2.i := R_1.i * F.s \} \quad Q_2 \{ R_1.s := R_2.s \}$$

Expressions: Multiplication 3/4

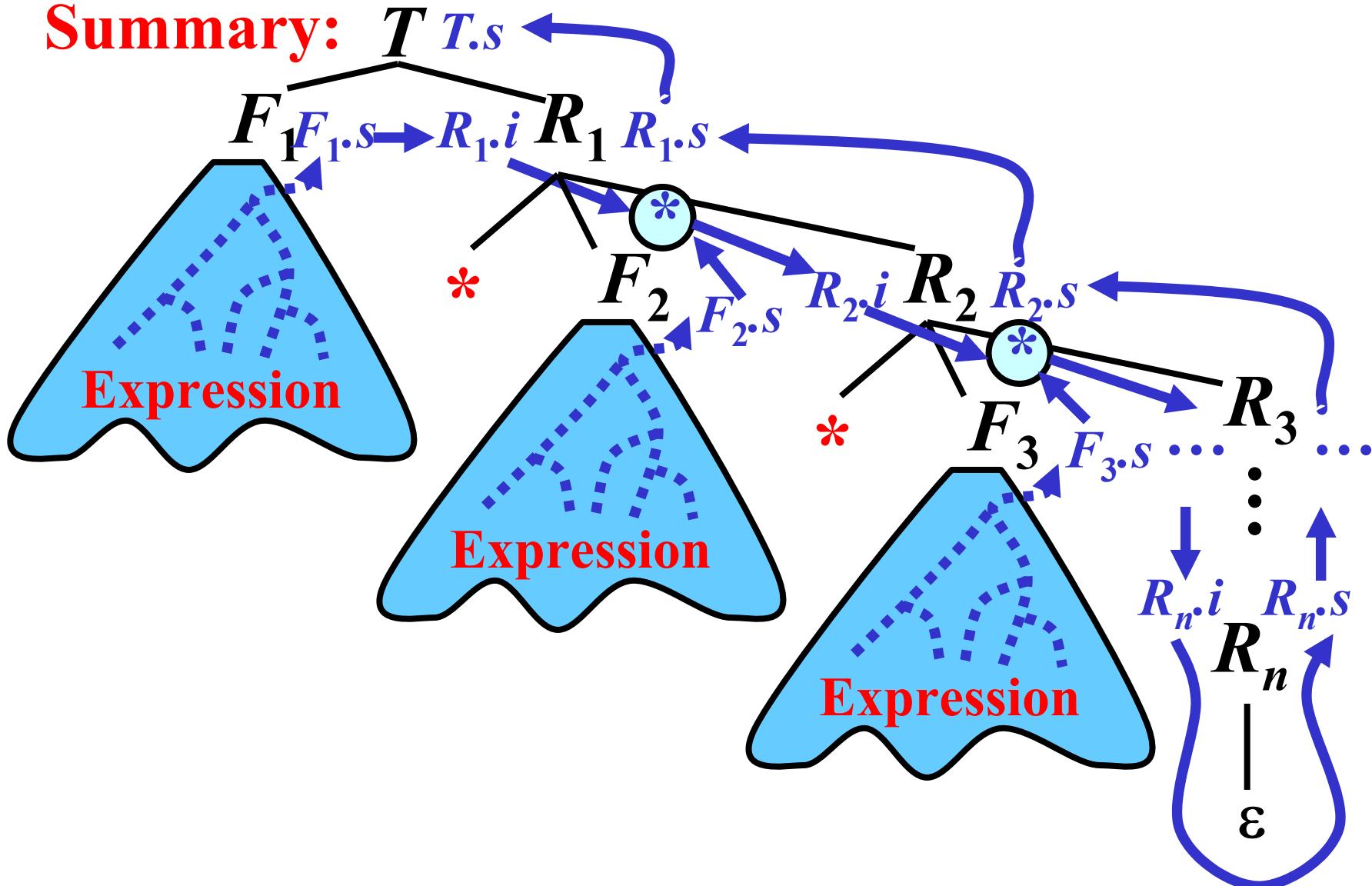
III.



$$R \rightarrow \varepsilon \quad \{R.s := R.i\}$$

Expressions: Multiplication 4/4

Summary:



Grammar for Expressions: Summary

1. $E \rightarrow T \{Q.i := T.s\} Q \{E.s := Q.s\}$
2. $Q_1 \rightarrow +T \{Q_2.i := Q_1.i + T.s\} Q_2 \{Q_1.s := Q_2.s\}$
3. $Q \rightarrow \varepsilon \{Q.s := Q.i\}$
4. $T \rightarrow F \{R.i := F.s\} R \{T.s := R.s\}$
5. $R_1 \rightarrow *F \{R_2.i := R_1.i * F.s\} R_2 \{R_1.s := R_2.s\}$
6. $R \rightarrow \varepsilon \{R.s := R.i\}$
7. $F \rightarrow (E \{F.s := E.s\})$
8. $F \rightarrow i \{F.s := i.value\}$

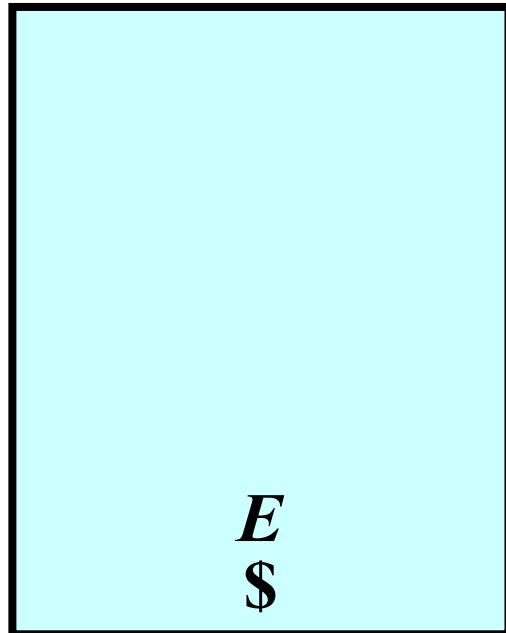
Evaluation of Expressions: Example 1/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_1 + i_2 \$$

Rule: $E \rightarrow T_1 \{Q_1.i := T_1.s\} Q_1 \{E.s := Q_1.s\}$

Parser pushdown:



Semantic pushdown:

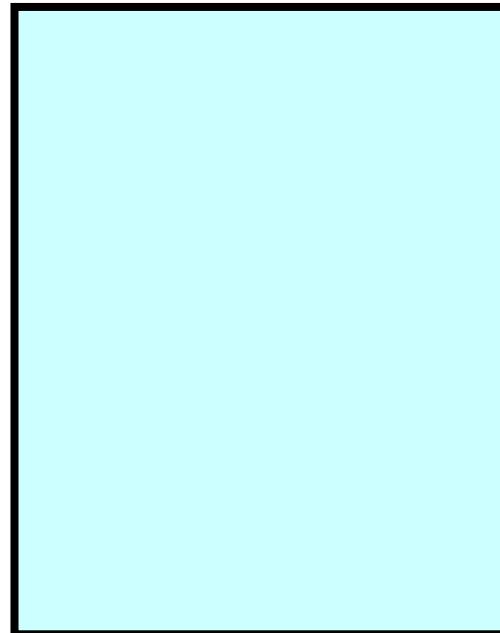


Illustration:



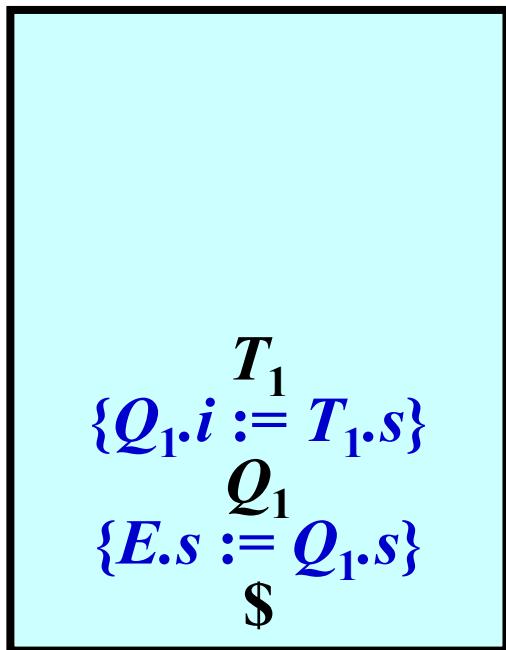
Evaluation of Expressions: Example 2/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_1 + i_2 \$$

Rule: $T_1 \rightarrow F_1 \{R_1.i := F_1.s\} R_1 \{T_1.s := R_1.s\}$

Parser pushdown:



Semantic pushdown:

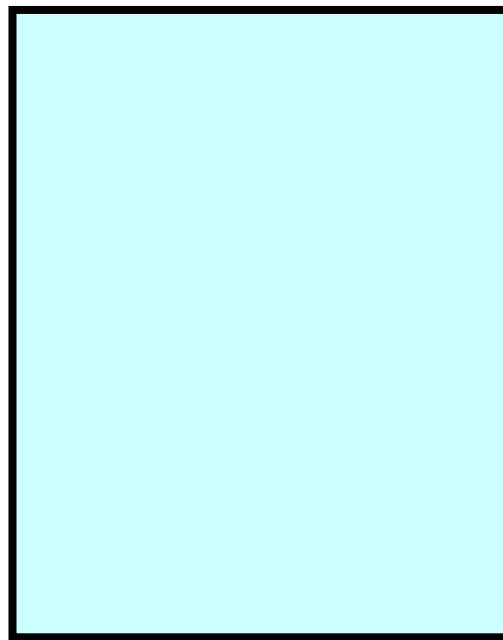
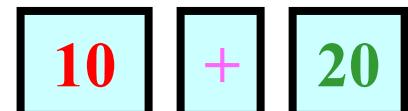
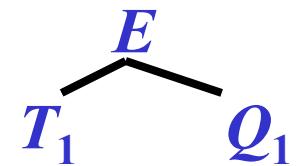


Illustration:



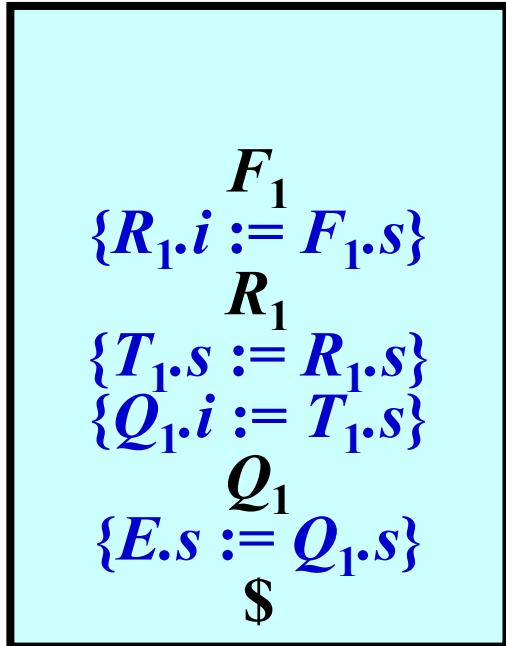
Evaluation of Expressions: Example 3/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_1 + i_2 \$$

Rule: $F_1 \rightarrow i_1 \{F_1.s := i.value\}$

Parser pushdown:



Semantic pushdown:

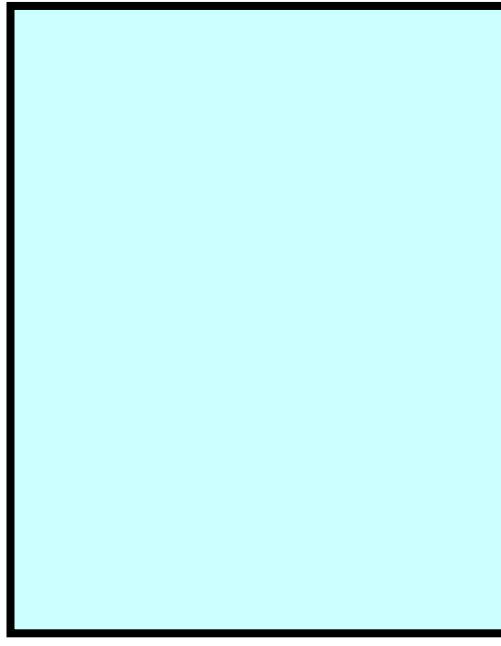
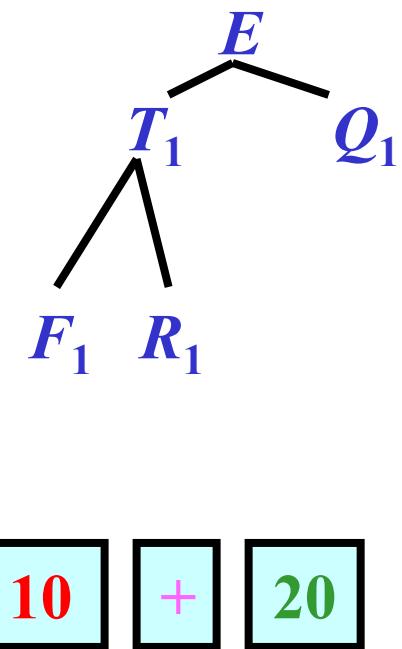


Illustration:



Evaluation of Expressions: Example 4/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_1 + i_2 \$$

Rule:

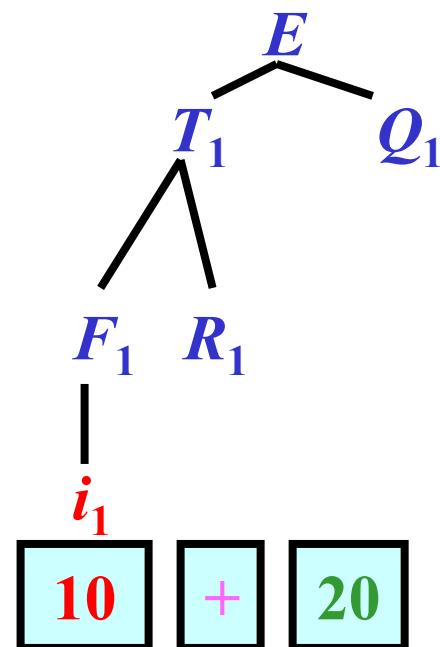
Parser pushdown:

```

 $i_1$ 
{ $F_1.s := i.value$ }
{ $R_1.i := F_1.s$ }
 $R_1$ 
{ $T_1.s := R_1.s$ }
{ $Q_1.i := T_1.s$ }
 $Q_1$ 
{ $E.s := Q_1.s$ }
$
```

Semantic pushdown:

Illustration:



Evaluation of Expressions: Example 5/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+ i_2 \$$

Rule:

Parser pushdown:

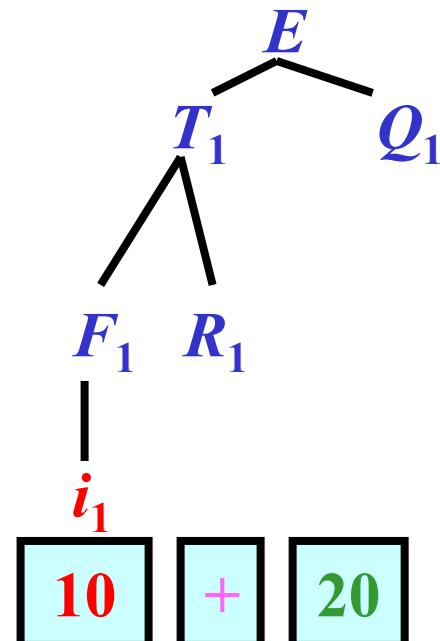
```

 $\{F_1.s := i.value\}$ 
 $\{R_1.i := F_1.s\}$ 
 $R_1$ 
 $\{T_1.s := R_1.s\}$ 
 $\{Q_1.i := T_1.s\}$ 
 $Q_1$ 
 $\{E.s := Q_1.s\}$ 
 $\$$ 

```

Semantic pushdown:

Illustration:



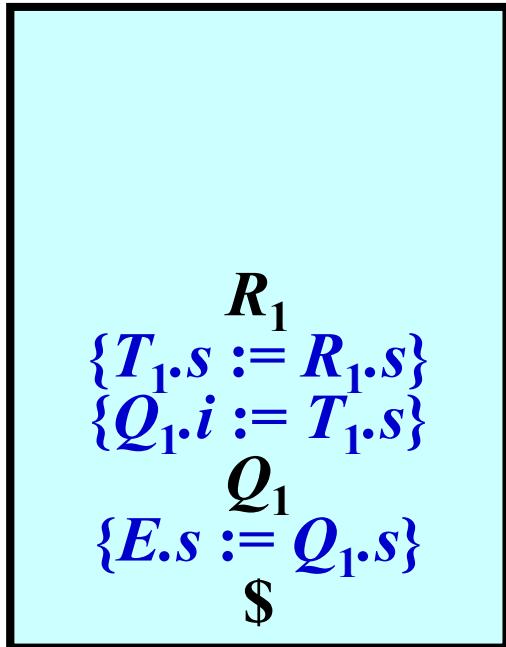
Evaluation of Expressions: Example 6/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+ i_2 \$$

Rule: $R_1 \rightarrow \varepsilon \{R_1.s := R_1.i\}$

Parser pushdown:



Semantic pushdown:

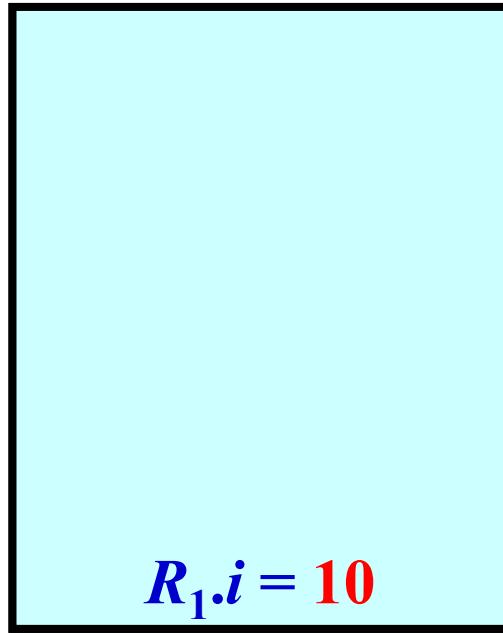
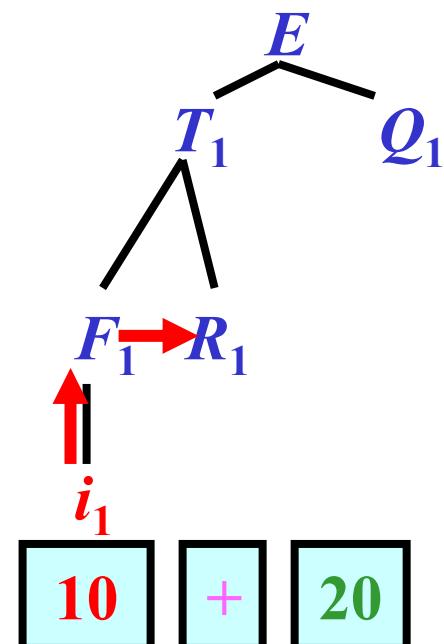


Illustration:



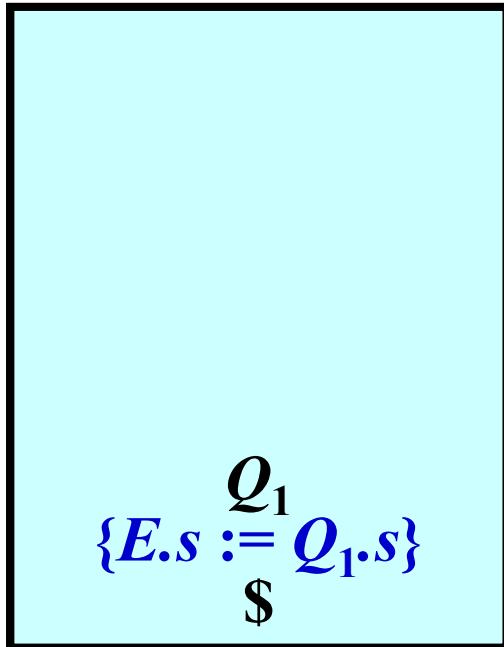
Evaluation of Expressions: Example 7/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+ i_2 \$$

Rule: $Q_1 \rightarrow +T_2 \{Q_2.i := Q_1.i + T_2.s\} Q_2 \{Q_1.s := Q_2.s\}$

Parser pushdown:



Semantic pushdown:

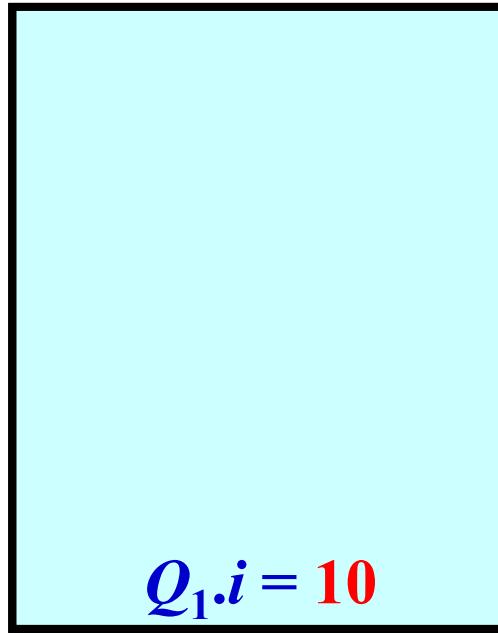
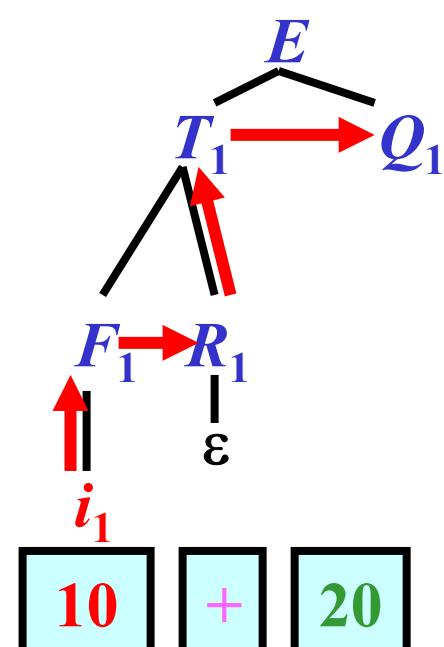


Illustration:



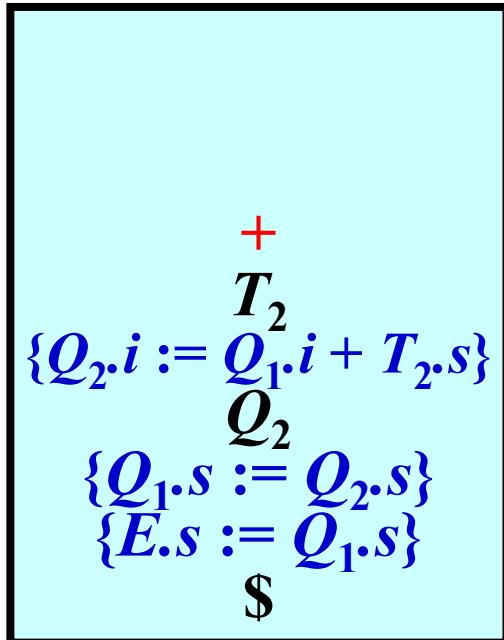
Evaluation of Expressions: Example 8/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+ i_2 \$$

Rule:

Parser pushdown:



Semantic pushdown:

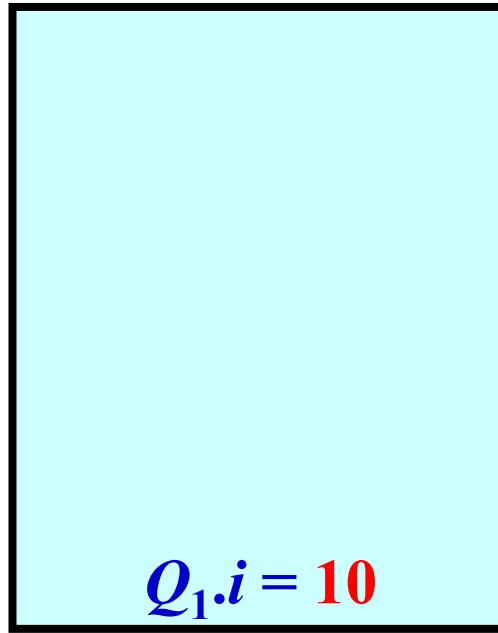
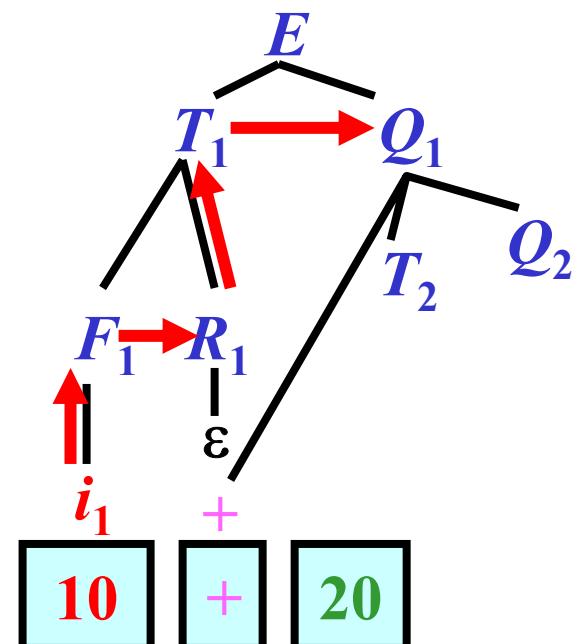


Illustration:



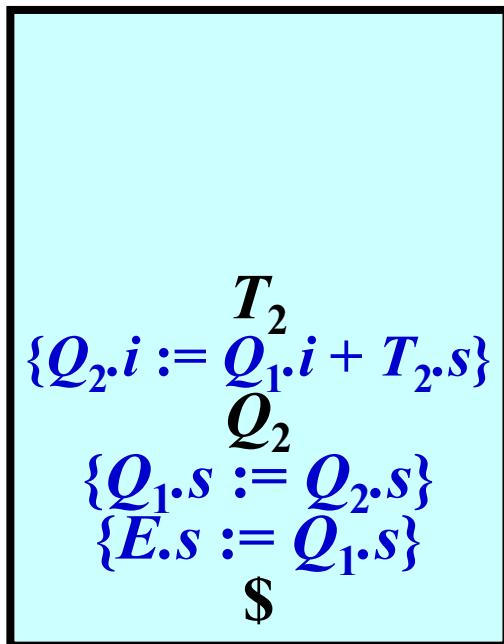
Evaluation of Expressions: Example 9/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_2 \$$

Rule: $T_2 \rightarrow F_2 \{R_2.i := F_2.s\} R_2 \{T_2.s := R_2.s\}$

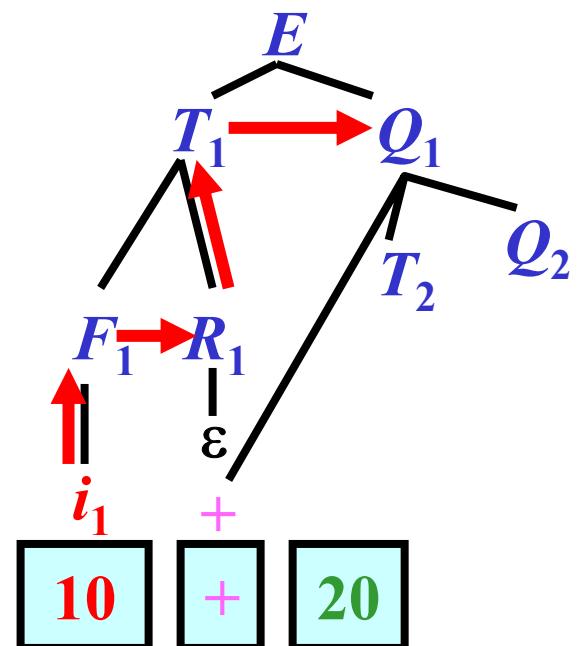
Parser pushdown:



Semantic pushdown:



Illustration:



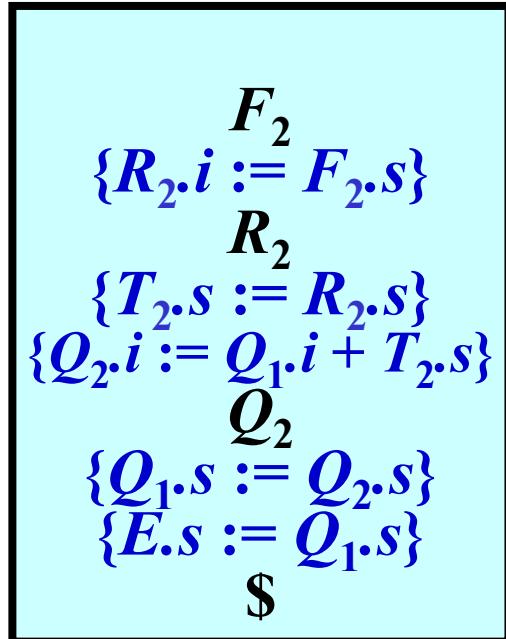
Evaluation of Expressions: Example 10/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_2 \$$

Rule: $F_2 \rightarrow i_2 \{F_2.s := i.value\}$

Parser pushdown:



Semantic pushdown:

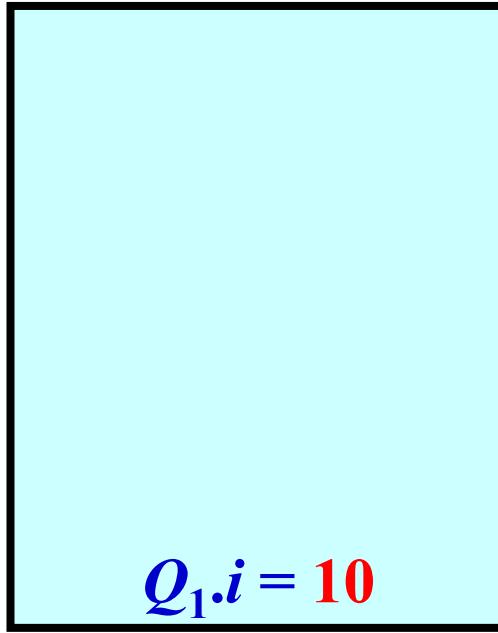
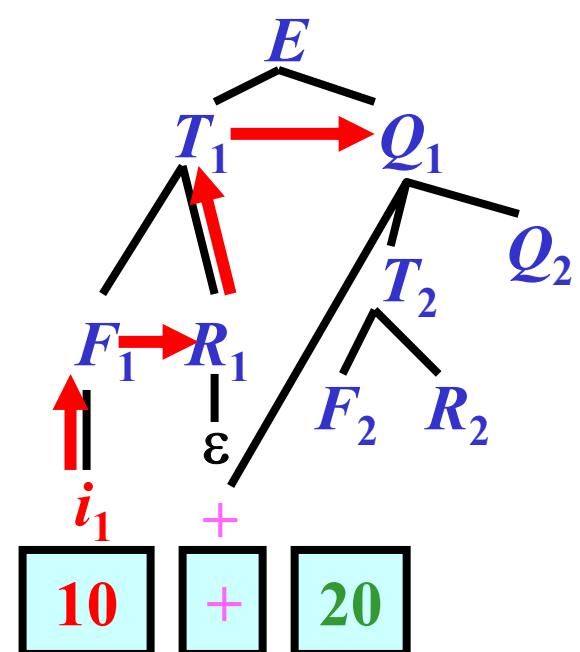


Illustration:



Evaluation of Expressions: Example 11/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_2 \$$

Rule:

Parser pushdown:

```

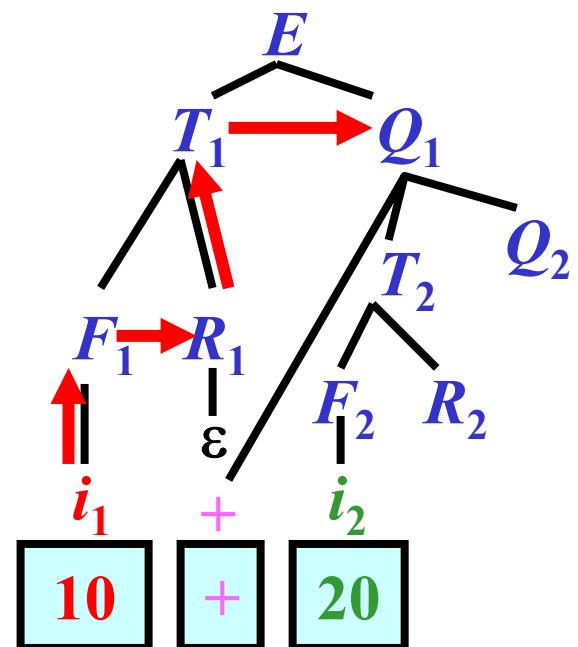
 $i_2$ 
{ $F_2.s := i.value$ }
{ $R_2.i := F_2.s$ }  $R_2$ 
{ $T_2.s := R_2.s$ }
{ $Q_2.i := Q_1.i + T_2.s$ }  $Q_2$ 
{ $Q_1.s := Q_2.s$ }
{ $E.s := Q_1.s$ }  $\$$ 

```

Semantic pushdown:

$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 12/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: \$

Rule:

Parser pushdown:

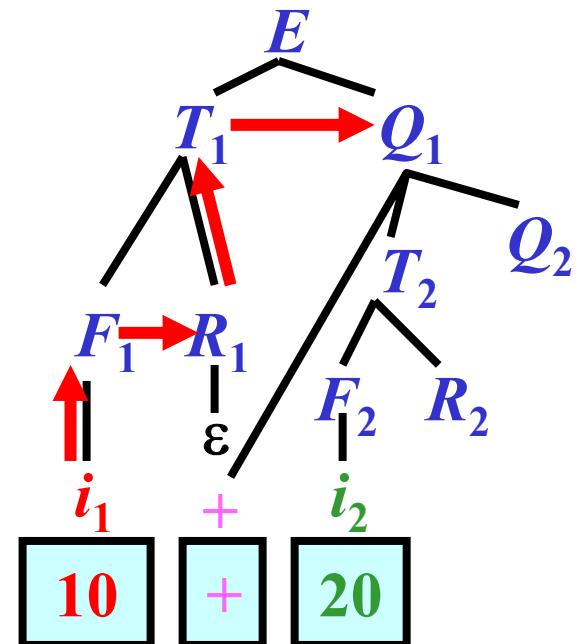
```

 $\{F_2.s := i.value\}$ 
 $\{R_2.i := F_2.s\}$ 
 $R_2$ 
 $\{T_2.s := R_2.s\}$ 
 $\{Q_2.i := Q_1.i + T_2.s\}$ 
 $Q_2$ 
 $\{Q_1.s := Q_2.s\}$ 
 $E.s := Q_1.s\}$ 
 $Q_1$ 
$
```

Semantic pushdown:

$Q_1.i = 10$

Illustration:



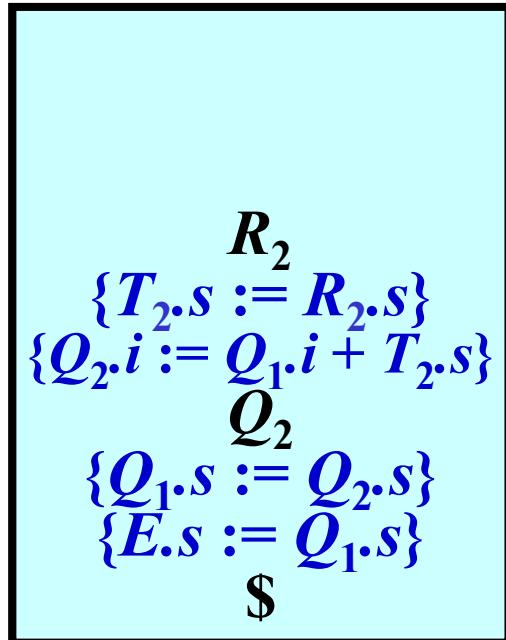
Evaluation of Expressions: Example 13/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: \$

Rule: $R_2 \rightarrow \varepsilon \{R_2.s := R_2.i\}$

Parser pushdown:



Semantic pushdown:

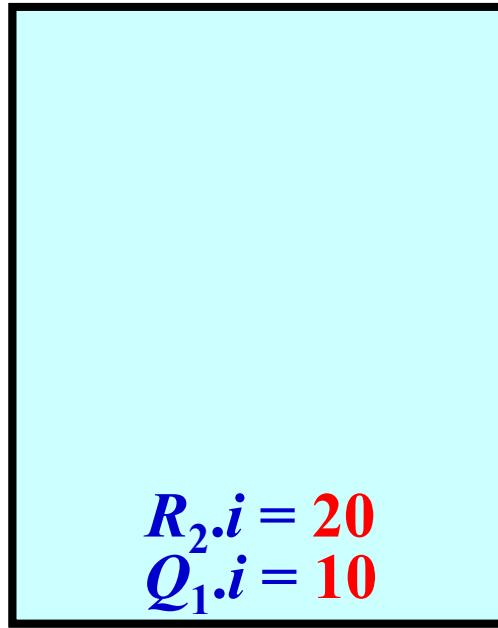
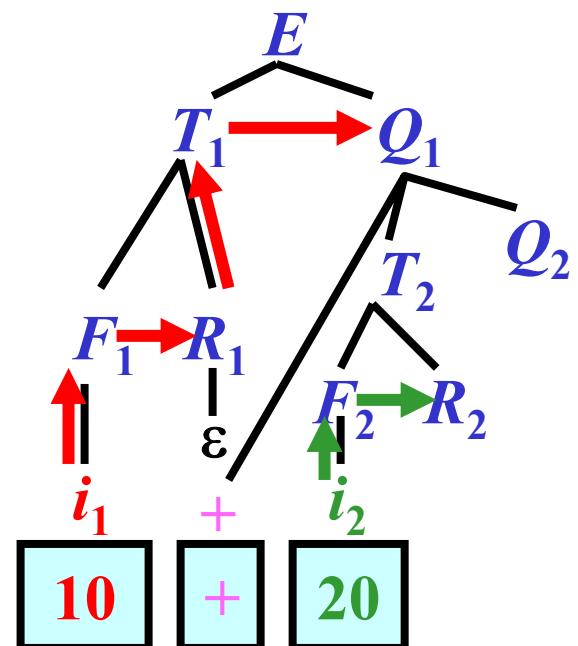


Illustration:



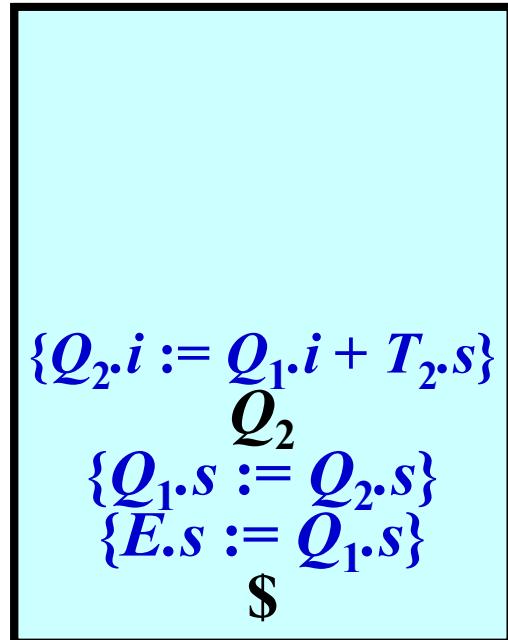
Evaluation of Expressions: Example 14/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: \$

Rule:

Parser pushdown:



Semantic pushdown:

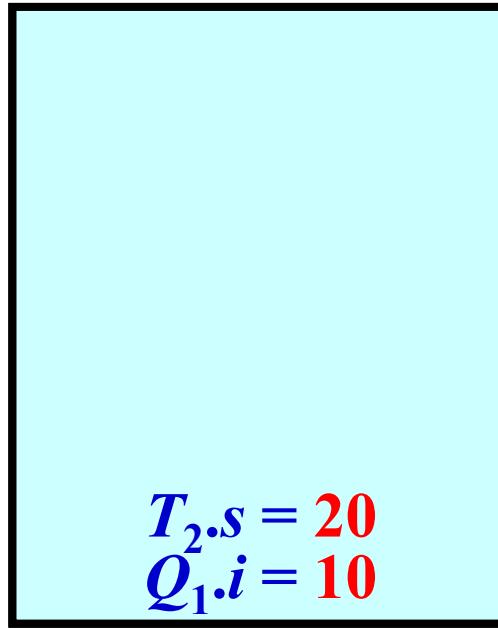
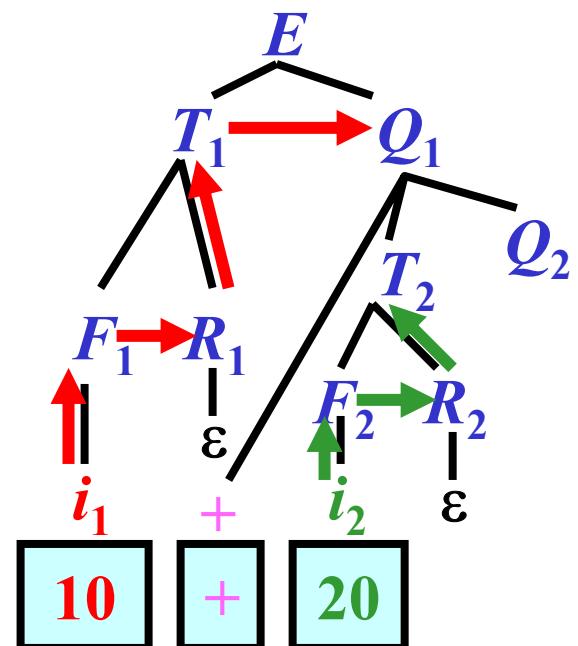


Illustration:



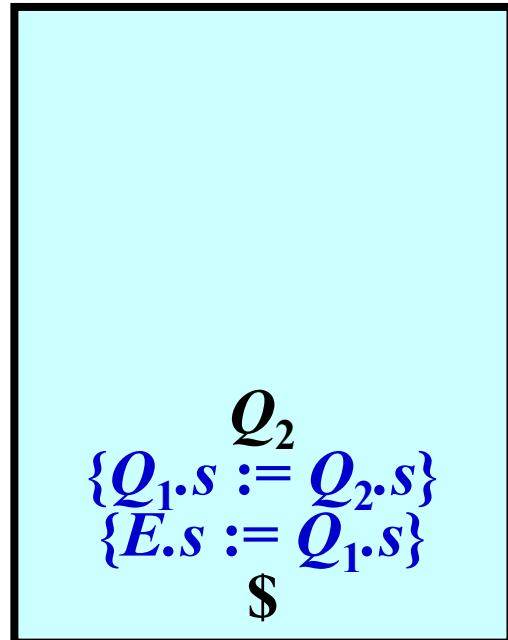
Evaluation of Expressions: Example 15/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: \$

Rule: $Q_2 \rightarrow \varepsilon \{Q_2.s := Q_2.i\}$

Parser pushdown:



Semantic pushdown:

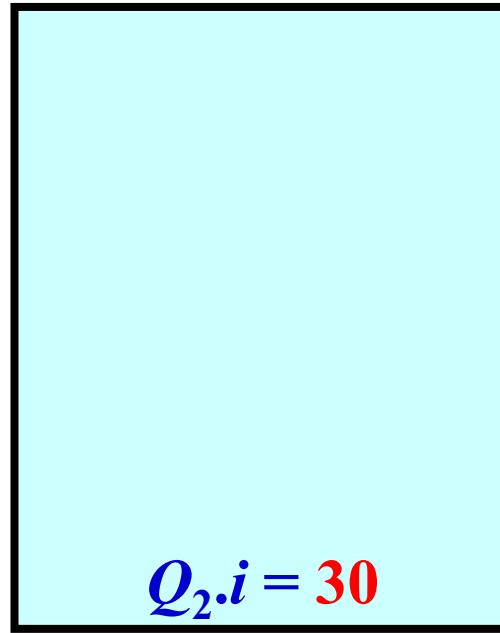
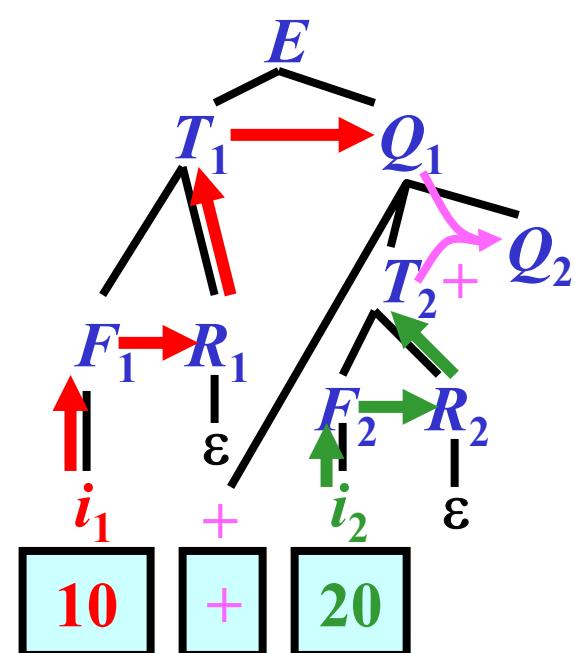


Illustration:



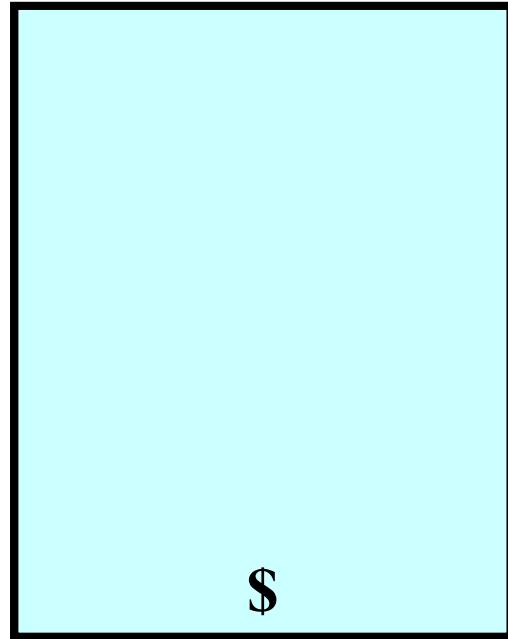
Evaluation of Expressions: Example 16/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: \$

Rule:

Parser pushdown:



Semantic pushdown:

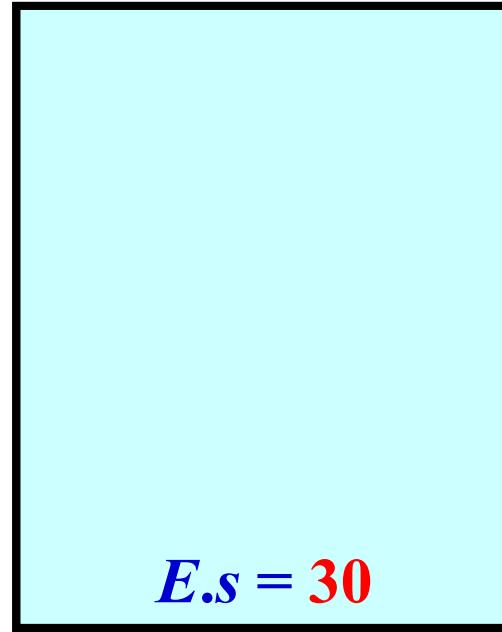
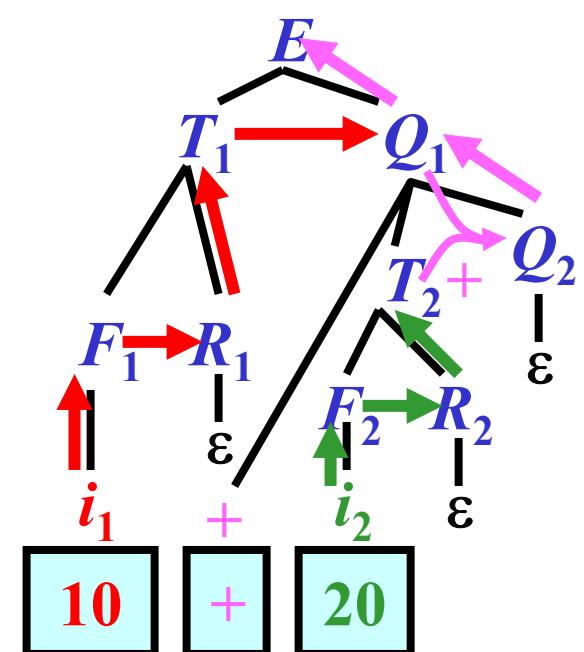


Illustration:



Semantic Analysis: Type Checking

1) Rule: E

$$\begin{array}{c} | \\ id \end{array}$$

Action:

$$E.type := id.type$$

2) Rule: E

$$\begin{array}{c} / \quad \backslash \\ E_1 \quad op \quad E_2 \end{array}$$

Operation **op** is
defined over types:

$$t_1 \text{ op } t_2 \rightarrow t_3$$

Action:

if ($E_1.type = t_1$ or
 $E_1.type$ is convertable to t_1)
and
($E_2.type = t_2$ or
 $E_2.type$ is convertable to t_2)
then
 $E.type := t_3$
else
Semantic Error.

Type Checking: Example 1/3

- Make a type-checking for a grammar:
- $G_{expr1} = (N, T, P, E)$, where $N = \{E, F, T\}$, $T = \{i, +, *, (,)\}$,
 $P = \{ E \rightarrow E+T, E \rightarrow T, T \rightarrow T^*F, T \rightarrow F, F \rightarrow (E), F \rightarrow i \}$
- Operators $*$, $+$ are defined as:

- int * int → int
- int + int → int
- real * real → real
- real + real → real

Possible Conversion:

- From int to real

Rule: $F \rightarrow i$

$\{F.type := i.type;$
 $\text{generate}(:=, i.loc, , F.loc) \}$

Rule: $F_i \rightarrow (E_j)$

$\{F_i.type := E_j.type\}$

Rule: $T_i \rightarrow F_j$

$\{T_i.type := F_j.type\}$

Rule: $E_i \rightarrow T_j$

$\{E_i.type := T_j.type\}$

Type Checking: Example 2/3

Rule: $E_i \rightarrow E_j + T_k \{$ if $E_j.type = T_k.type$ then begin
 $E_i.type := E_j.type$
 generate(+, $E_j.loc$, $T_k.loc$, $E_i.loc$)
 end
 else begin
 generate(*new.loc*, h , ,)
 if $E_j.type = int$ then begin
 generate(*int-to-real*, $E_j.loc$, , h)
 generate(+, h , $T_k.loc$, $E_i.loc$)
 end
 else begin
 generate(*int-to-real*, $T_k.loc$, , h)
 generate(+, $E_j.loc$, h , $E_i.loc$)
 end
 $E_i.type := real$
 end
 }

Type Checking: Example 3/3

Rule: $T_i \rightarrow T_j^* F_k \{$ if $T_j.type = F_k.type$ then begin
 $T_i.type := T_j.type$
 generate(*, $T_j.loc$, $F_k.loc$, $T_i.loc$)
 end
 else begin
 generate(new.loc, h , ,)
 if $T_j.type = int$ then begin
 generate(int-to-real, $T_j.loc$, , h)
 generate(*, h , $F_k.loc$, $T_i.loc$)
 end
 else begin
 generate(int-to-real, $F_k.loc$, , h)
 generate(*, $T_j.loc$, h , $T_i.loc$)
 end
 $T_i.type := real$
 end
 }

Short Evaluation (Jumping Code)

Idea:

- $a = \text{true}$ implies $a \text{ or } (\dots ? \dots) = \text{true}$
- $a = \text{false}$ implies $a \text{ and } (\dots ? \dots) = \text{false}$

Note: $(\dots ? \dots)$ is not evaluated.

1) $(a \text{ and } b) = p$:

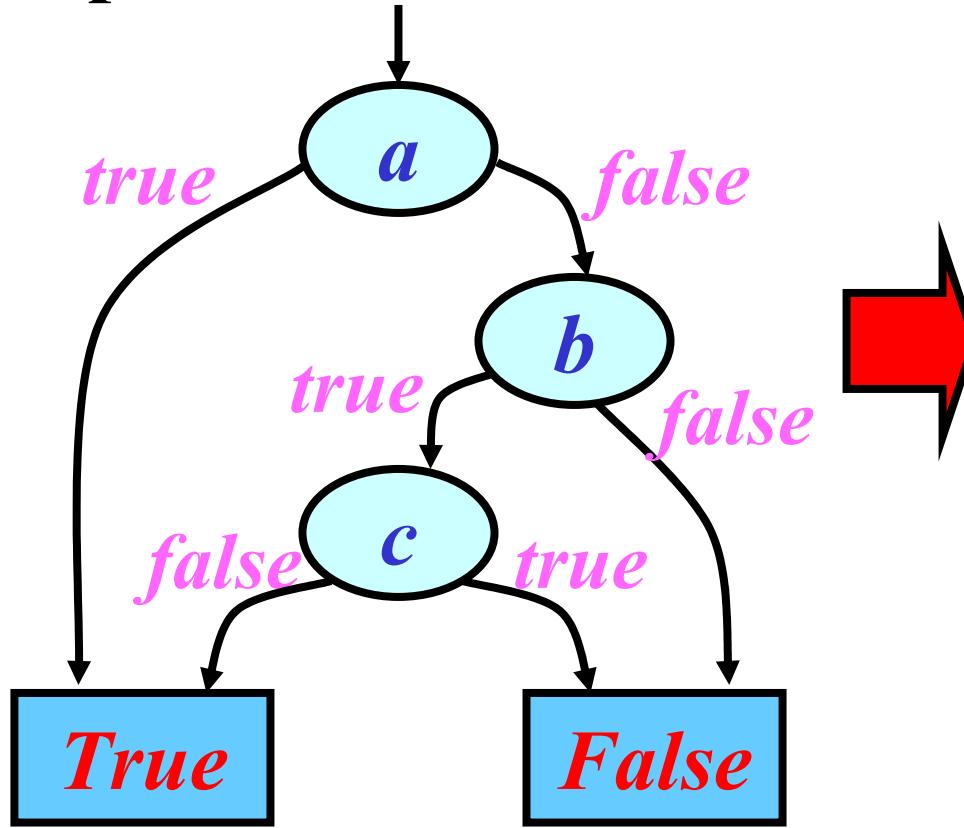
if $a = \text{false}$ then $p = \text{false}$
else $p = b$

2) $(a \text{ or } b) = p$:

if $a = \text{true}$ then $p = \text{true}$
else $p = b$

Short Evaluation: Graphic Representation

Example: *a or (b and (not c))*:



```

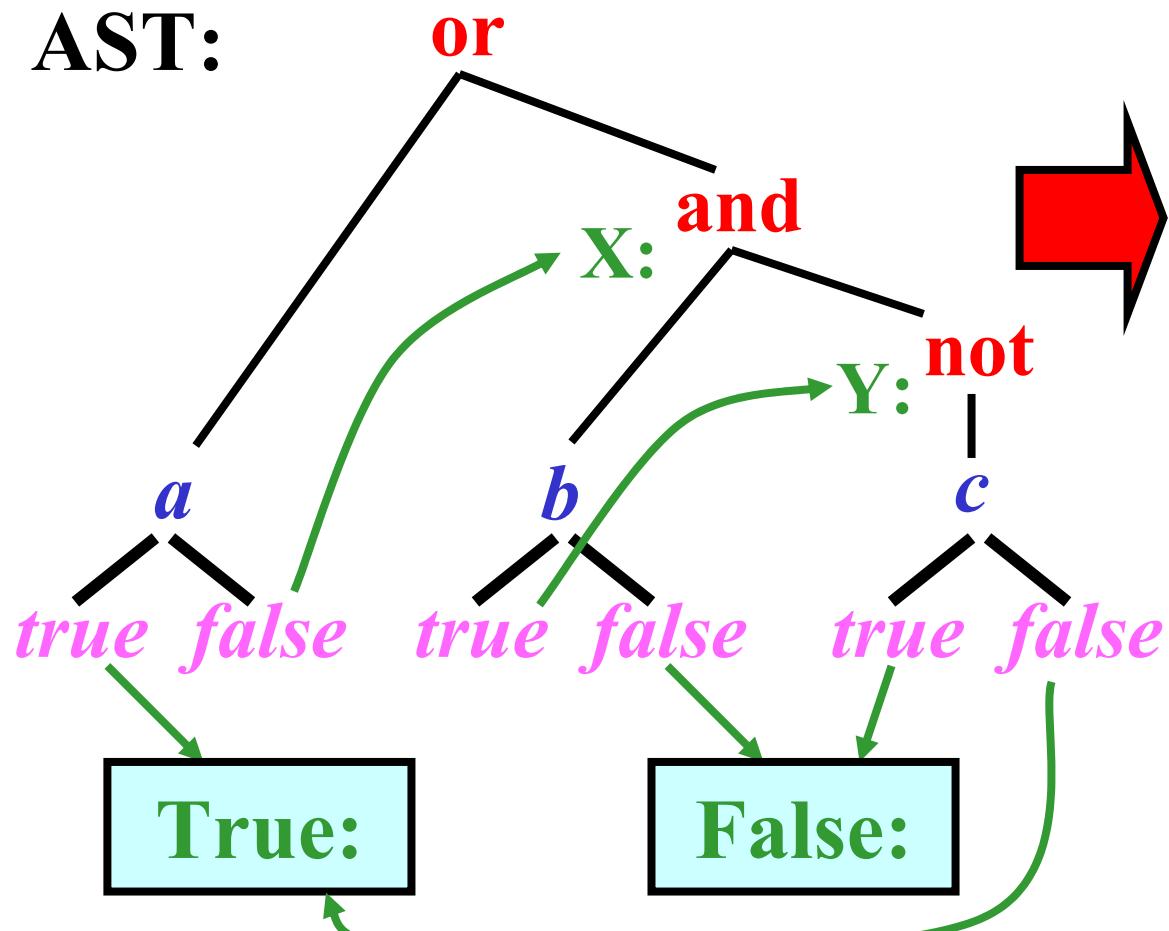
if a goto True
goto X
X:
if b goto Y
goto False
Y:
if c goto False
goto True
True: ...
False: ...
  
```

- Simulation of this graphic representation by 3AC jumps

Short Evaluation Using AST: Introduction

Example: ***a or (b and (not c))***:

AST:



```

if a goto True
goto X

X:
if b goto Y
goto False

Y:
if c goto False
goto True

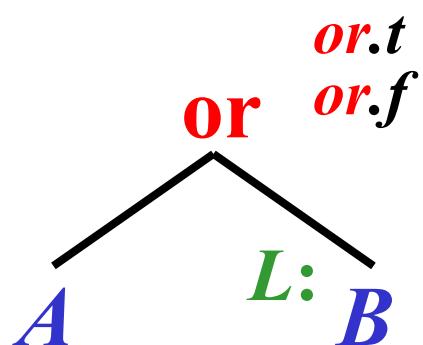
True: ...
False: ...
  
```

Short Evaluation Using AST: Implementation

- Every AST node, X , has assigned two attributes $X.t, X.f$

Elementary ASTs:

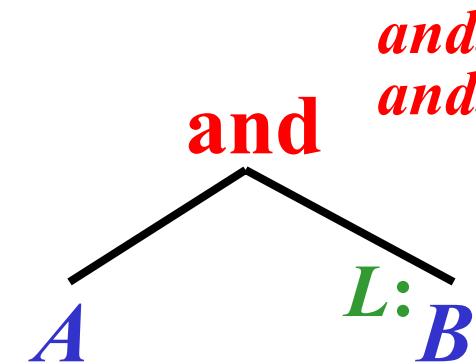
1)



$$\begin{aligned} A.t &:= \textcolor{red}{or.t} & B.t &:= \textcolor{red}{or.t} \\ A.f &:= \textcolor{green}{L} & B.f &:= \textcolor{red}{or.f} \end{aligned}$$

• Note: L = a new label

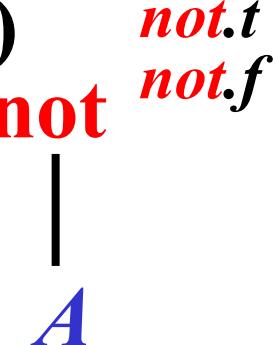
2)



$$\begin{aligned} A.t &:= \textcolor{green}{L} & B.t &:= \textcolor{red}{and.t} \\ A.f &:= \textcolor{red}{and.f} & B.f &:= \textcolor{red}{and.f} \end{aligned}$$

• Note: L = a new label

3)



$$\begin{aligned} A.t &:= \textcolor{red}{not.f} \\ A.f &:= \textcolor{red}{not.t} \end{aligned}$$

- Initialization: Let R is the root of AST, then:

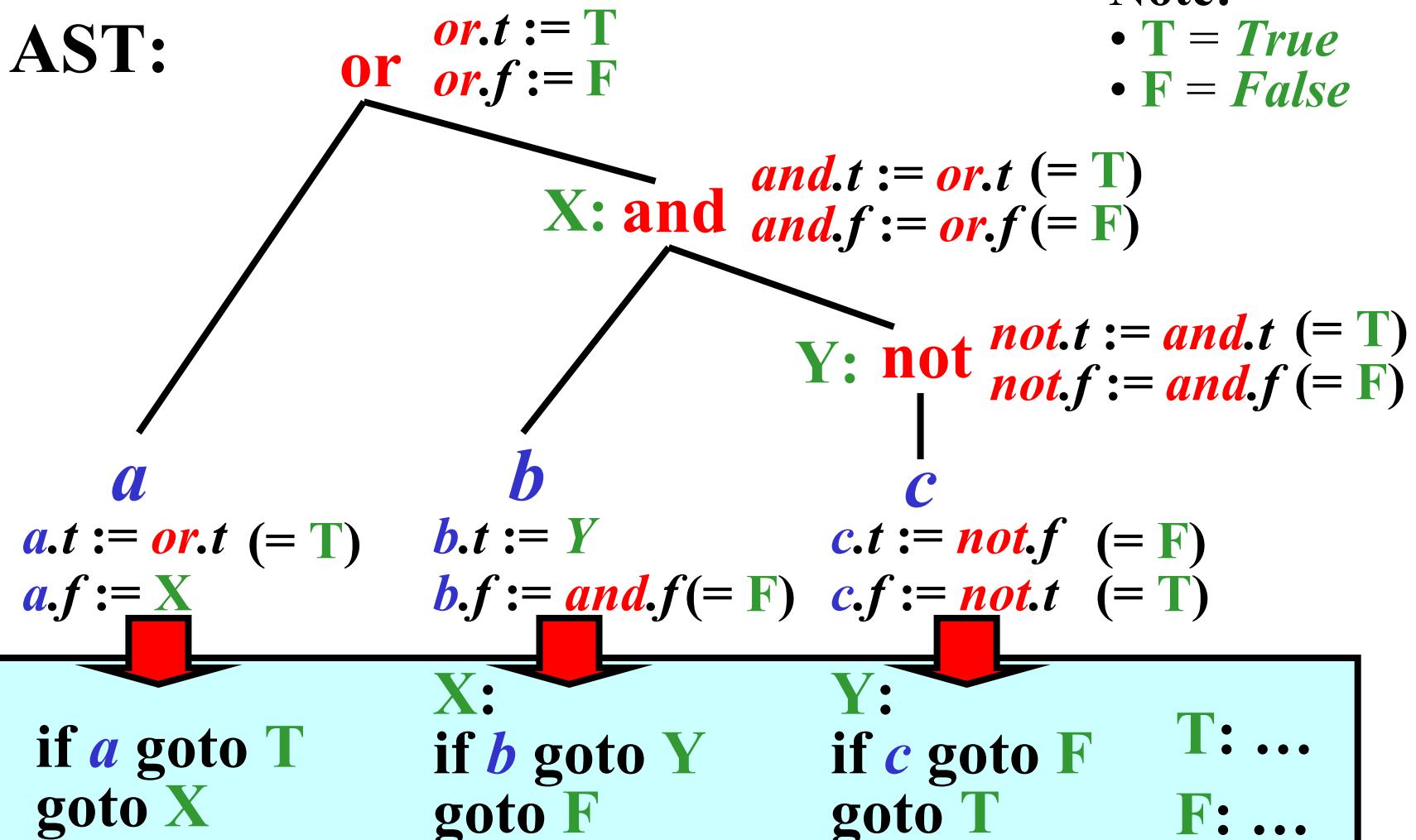
$R.t := \text{True}, R.f := \text{False}$ (**True** & **False** are labels)

- Propagation: Attributes are propagated from root to leaves in AST using rules 1), 2) and 3).

Short Evaluation Using AST: Example

Example: ***a or (b and (not c))***:

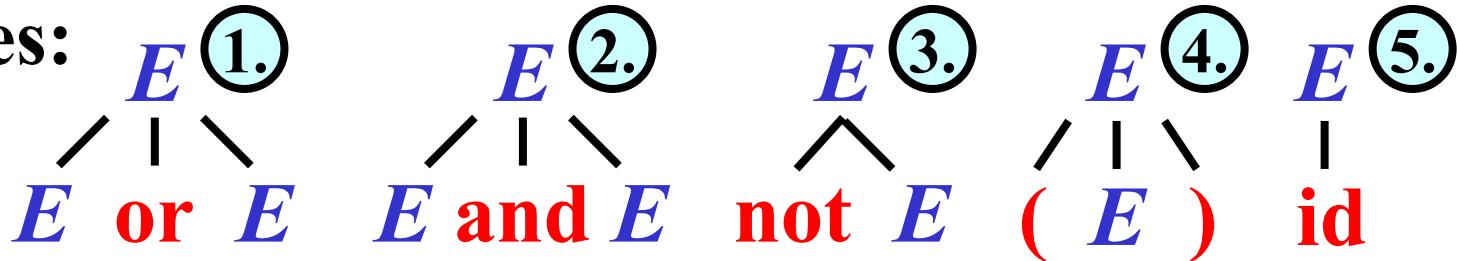
AST:



Short Evaluation: Direct Code Generation 1/5

- Grammar for boolean expressions:

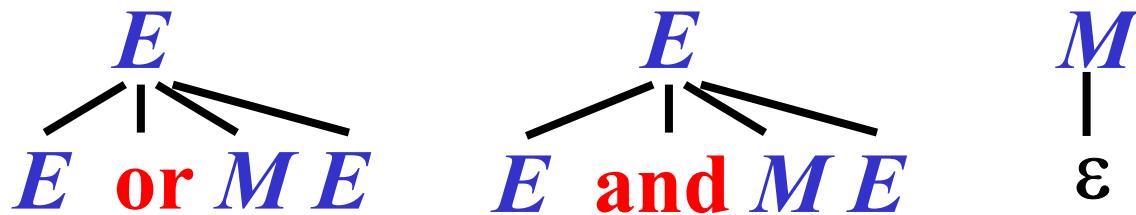
Rules:



Note: Ambiguity!

- Modification of grammar:

1) Replace rules ①.& ②. with:



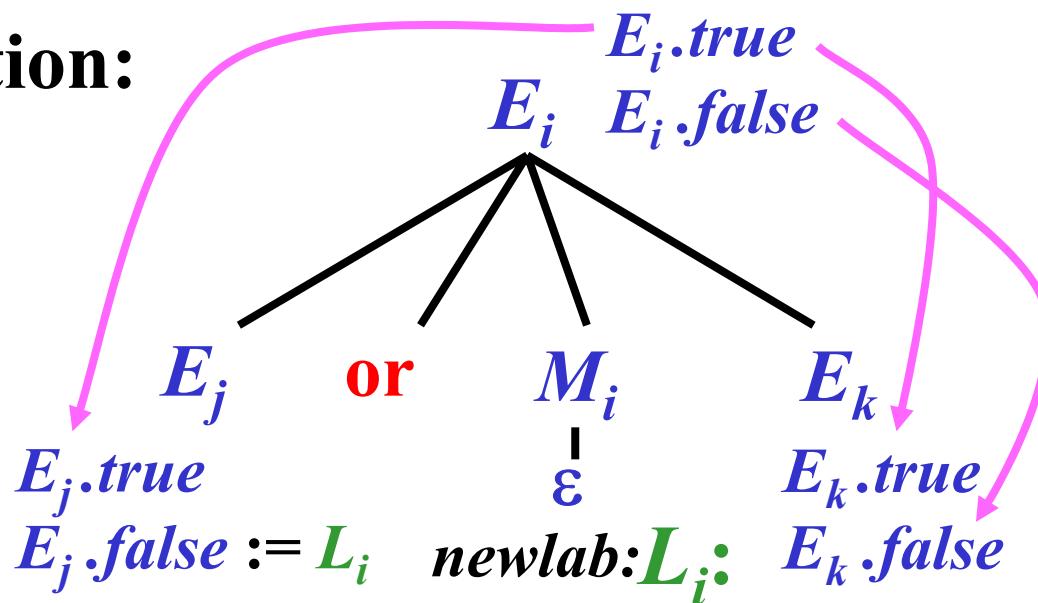
2) Assign to each rule the following semantic action

Short Evaluation: Direct Code Generation 2/5

$M_i \rightarrow \varepsilon \quad \{\text{generate "M}_i.\text{lab:}\}\} // \text{Generation of a new label}$

$E_i \rightarrow E_j \text{ or } M_i E_k \quad \{M_i.\text{lab} := \text{GenerateNewLab};$
 $E_j.\text{true} := E_i.\text{true}; E_j.\text{false} := M_i.\text{lab}$
 $E_k.\text{true} := E_i.\text{true}; E_k.\text{false} := E_i.\text{false} \}$

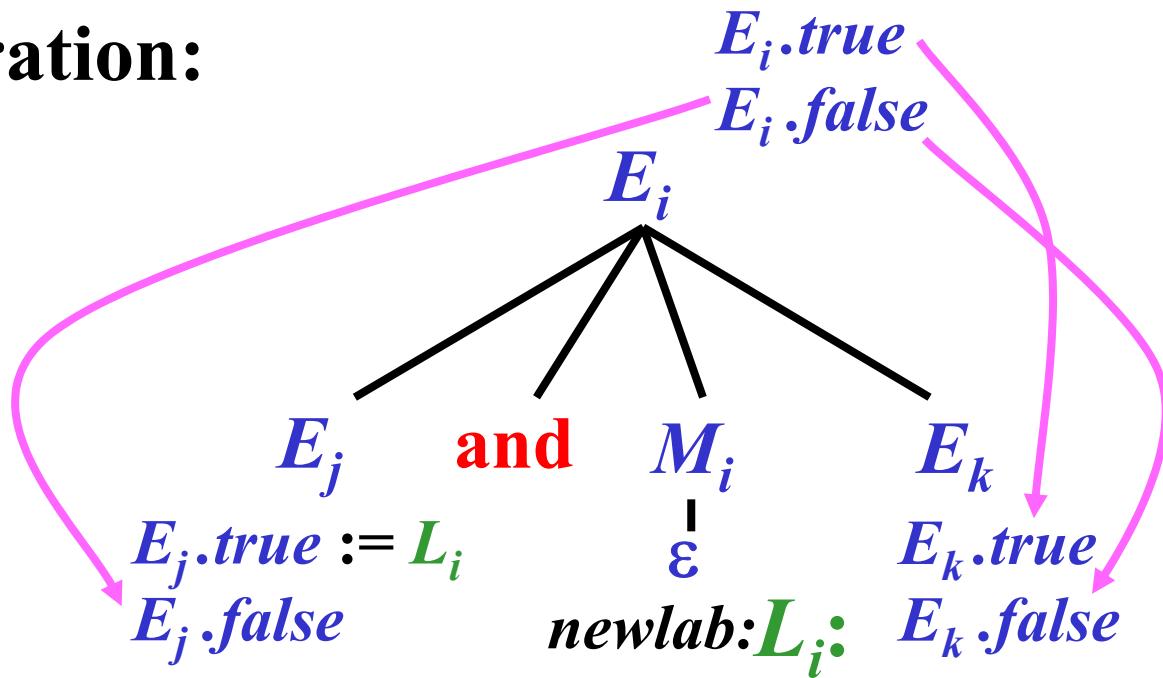
Illustration:



Short Evaluation: Direct Code Generation 3/5

$E_i \rightarrow E_j \text{ and } M_i E_k \{ M_i.lab := GenerateNewLab;$
 $E_j.true := M_i.lab; E_j.false := E_i.false$
 $E_k.true := E_i.true; E_k.false := E_i.false \}$

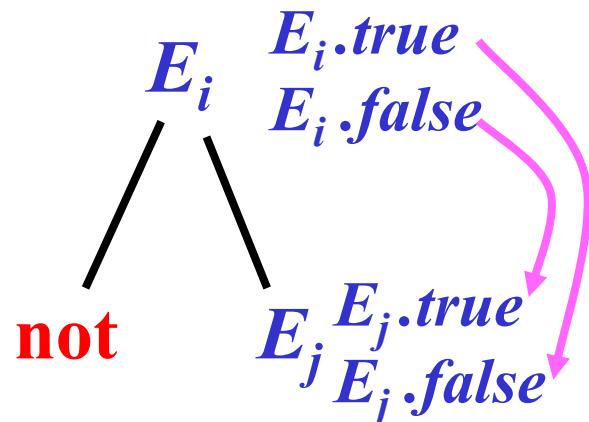
Illustration:



Short Evaluation: Direct Code Generation 4/5

$E_i \rightarrow \text{not } E_j \quad \{ \begin{array}{l} E_j.\text{true} := E_i.\text{false}; \\ E_j.\text{false} := E_i.\text{true} \end{array} \}$

Illustration:

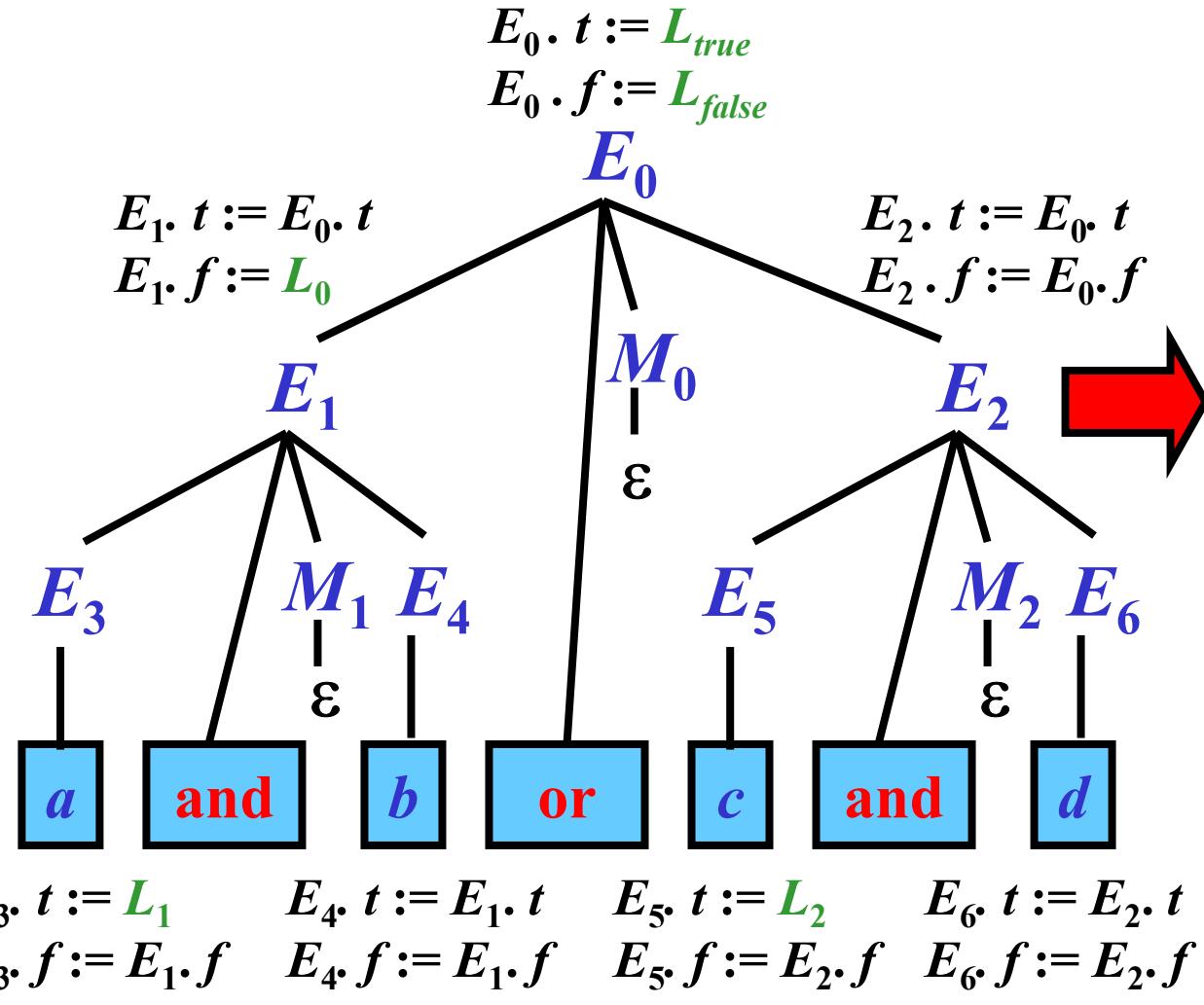


$$E_i \rightarrow (E_j) \quad \{ E_j.\textit{true} := E_i.\textit{true}; \\ E_j.\textit{false} := E_i.\textit{false} \}$$

$E_i \rightarrow id_j$ { generate “if $id_j.val$ goto $E_i.true$ ”;
 generate “goto $E_i.false$ ” }

Short Evaluation: Direct Code Generation 5/5

Example: *a and b or c and d*:

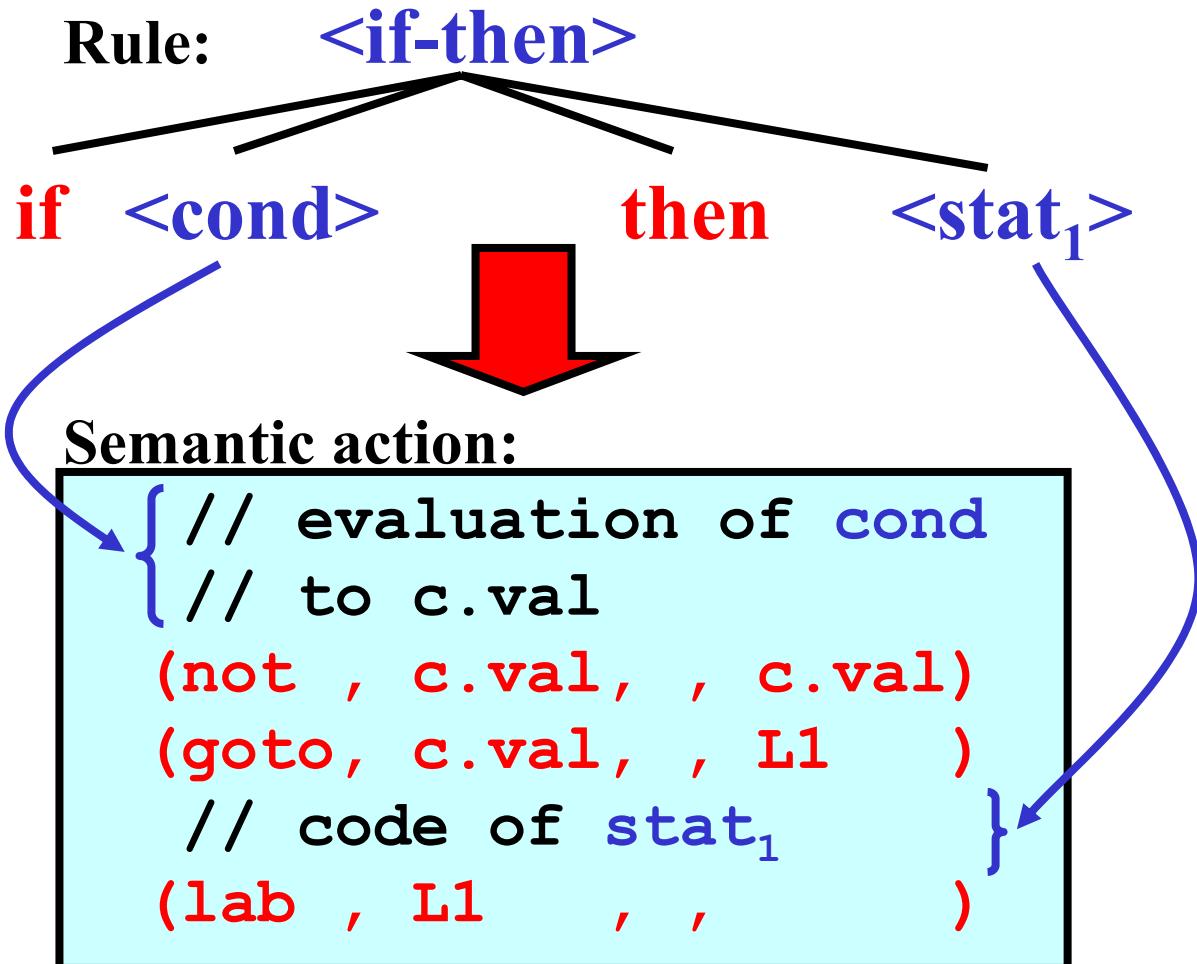


```

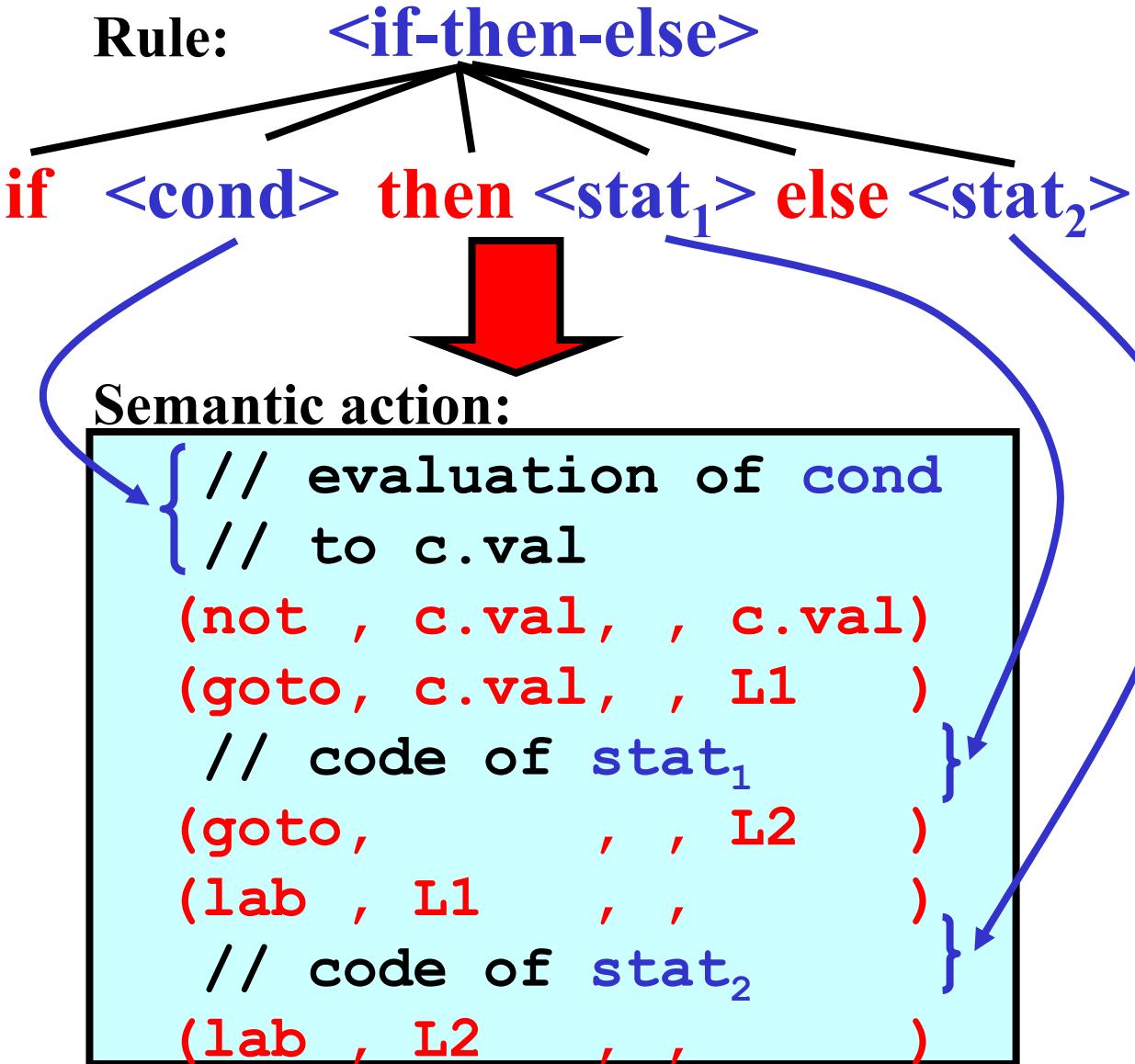
if a goto  $L_1$ 
goto  $L_0$ 
L_1:
if b goto  $L_{true}$ 
goto  $L_0$ 
L_0:
if c goto  $L_2$ 
goto  $L_{false}$ 
L_2:
if d goto  $L_{true}$ 
goto  $L_{false}$ 
L_{true}: ...
L_{false}: ...

```

Branching: If-Then



Branching: If-Then-Else



While Loop

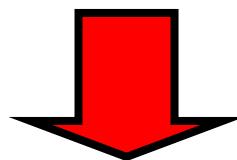
Rule: <while-loop>

while

<cond>

do

<stat>



Semantic action:

```
(lab , L1 , , )  
{ // evaluation of cond  
// to c.val  
(not , c.val, , c.val)  
(goto, c.val, , L2 )  
// code of stat }  
(goto, , , L1 )  
(lab , L2 , , )
```

Repeat Loop

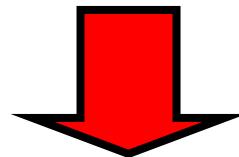
Rule: <repeat-loop>

repeat

<stat>

until

<cond>



Semantic action:

(lab , L1 , ,)

{// code of stat

// evaluation of cond}

// to c.val

(not , c.val, , c.val)

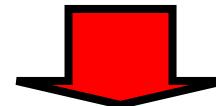
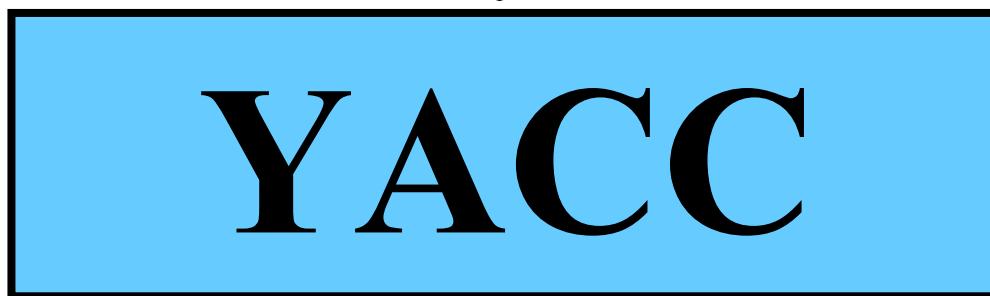
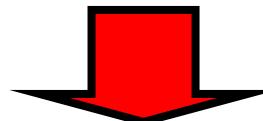
(goto, c.val, , L1)

Yacc: Basic Idea

- Automatic construction of **parser** from **CFG**
- Yacc compiler × Yacc language
- *Yacc* from *Yet another compiler compiler*

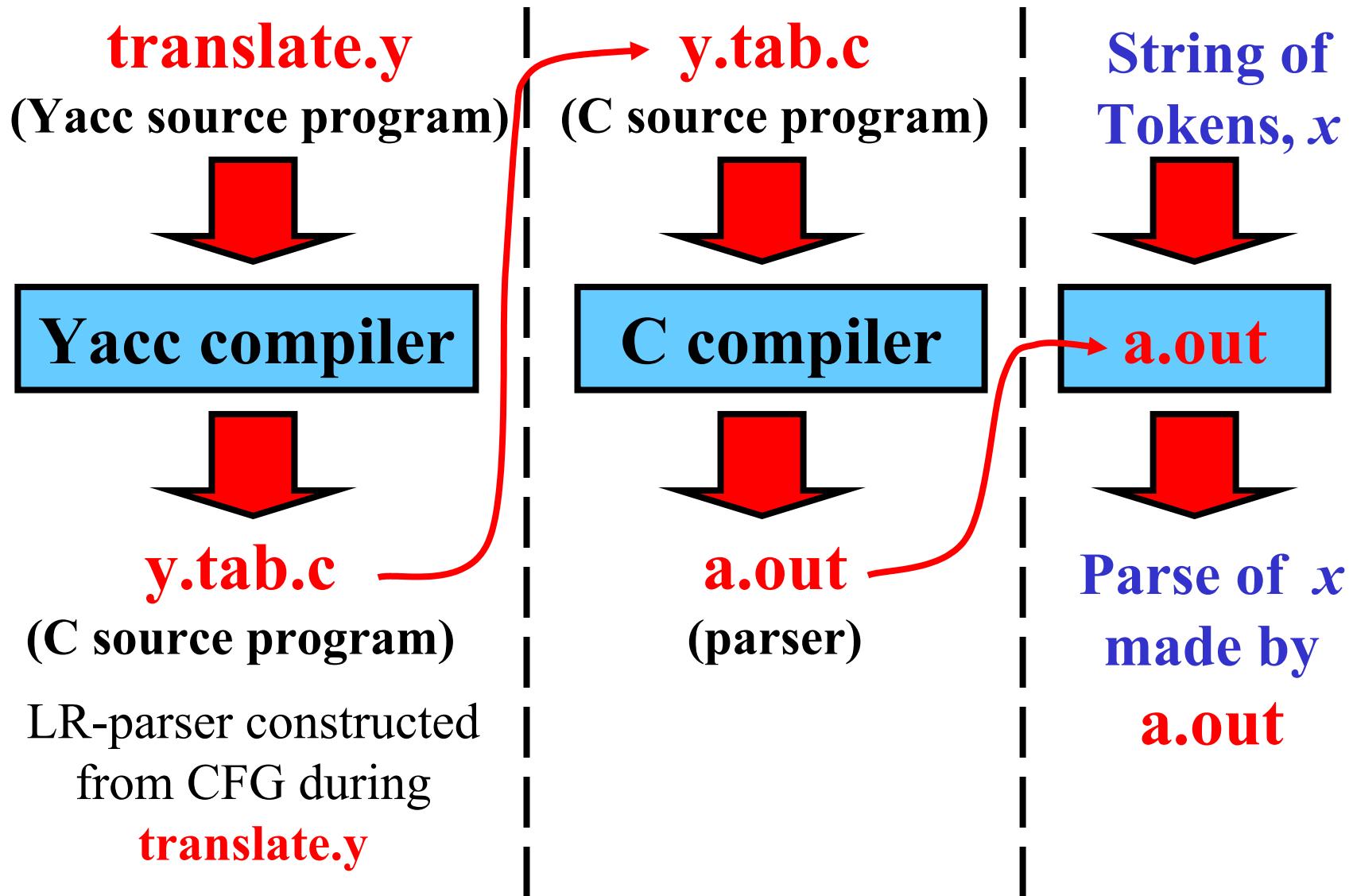
Illustrate:

Context-free grammar, G



Parser for G

Yacc: Phases of Compilation



Structure of Yacc Source Program

/* **Section I: Declaration** */

d₁, d₂, ... , d_i

%% /* End of Section I*/

/* **Section II: Translation rules** */

r₁, r₂, ... , r_j

%% /* End of Section II*/

/* **Section III: Auxiliary procedures** */

P₁, P₂, ... , P_k

Description of Grammar in Yacc

- **Nonterminals:** names (= strings)
- **Example:** `prog`, `stat`, `expr`, ...
- **Terminals:** Characters in quotes or declared tokens
- **Example:** `'+'`, `'*'`, `'('`, `')'`, `ID`, `INTEGER`

- **Rules:** Set of A -rules $\{ A \rightarrow x_1, A \rightarrow x_2, \dots A \rightarrow x_n \}$

is written as

$A : x_1$

| x_2

...

| x_n

- **Example:**

$expr : expr '+' expr$
| ID

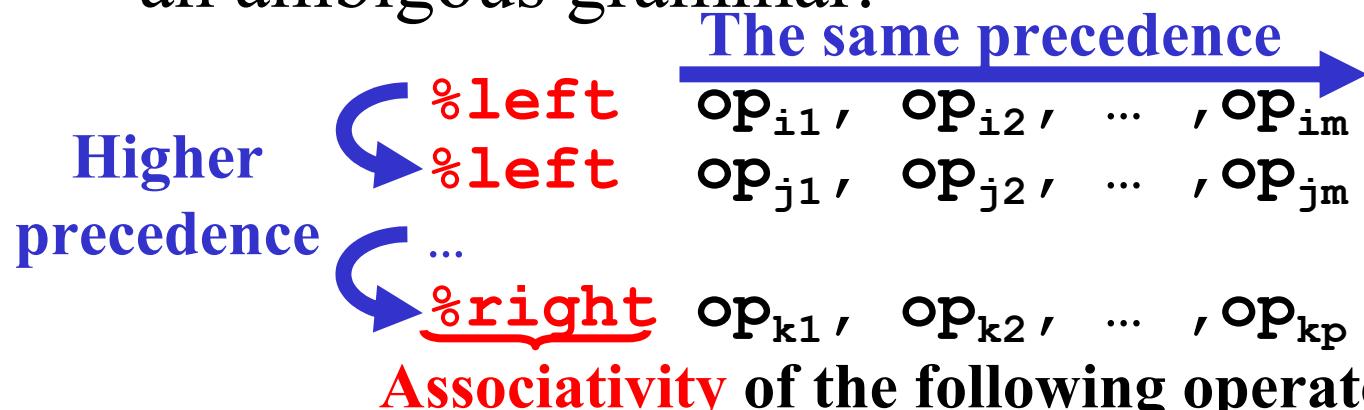
- **Start Nonterminal:** A left side of the first rule.

Section I: Declaration

1) Declaration of tokens

%token TYPE_OF_TOKEN

2) Specification of **associativity** & precedence in an ambiguous grammar.



Example:

```
%token INTEGER
%token ID
%left '+'
%left '*'
```

Section II: Translation Rules

- Translation rules are in the form:

Rule	Semantic_Action
-------------	------------------------

- **Semantic_Action** is a program routine that specifies what to do if **Rule** is used.

Special symbols for a rule, r :

$\$\$$ = attribute of r 's left-hand side

$\$i$ = attribute of the i -th symbols on r 's right-hand side

Example:

```
expr : expr '+' expr { $$ = $1 + $3 }
      | expr '*' expr { $$ = $1 * $3 }
      | '(' expr ')' { $$ = $2 }
      | INTEGER
      | ID
```

Section III: Auxiliary Procedures

- Auxiliary procedures used by translation rules

Note: If the Yacc-parser do not cooperate with a scanner (e.g. Lex), then there is **yylex()** implemented in this section.

Example:

```
int yylex() {  
    /* Get the next token */  
    &yyval = attribute;  
    return TYPE_OF_TOKEN;  
}
```

Complete Source Program in Yacc

```
%token INTEGER
```

```
%token ID
```

```
%left '+'
```

```
%left '*'
```

```
%%
```

```
expr : expr '+' expr { $$ = $1 + $3 }
```

```
    | expr '*' expr { $$ = $1 * $3 }
```

```
    | '(' expr ')' { $$ = $2 }
```

```
    | INTEGER
```

```
    | ID
```

```
%%
```

```
int yylex () { ... }
```